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[ ]: import numpy as np
import matplotlib
import matplotlib.pyplot as plt
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[ ]: mu = [0.2, 0.8]
# mu = [0.2, 0.4, 0.6, 0.8]

def SEA(alpha, T):
    t = 0
    A = [i for i in range(len(mu))]
    n = [0 for i in range(len(mu))]
    r = [0. for i in range(len(mu))]
    while t < T:
        for arm in A:
            r[arm] += mu[arm] + np.random.randn()
            n[arm] += 1
            t += 1
            if t >= T:
                return r, n
        if len(A) > 1:
            means = np.array([r[arm]/n[arm] for arm in A])
            bonus = np.array([alpha * np.sqrt(np.log(T)/n[arm]) for arm in A])
            upper = means + bonus
            lower_val = np.max(means - bonus)
            sign = upper > lower_val
            A = [A[i] for i in range(len(A)) if sign[i]]
    return r, n

def UCB(alpha, T):
    t = 0
    A = [i for i in range(len(mu))]
    n = [0 for i in range(len(mu))]
    r = [0. for i in range(len(mu))]
    while t < T:
        arm = np.argmax([r[arm]/(n[arm] + 1e-10) + \
                        alpha * np.sqrt(np.log(T)/(n[arm] + 1e-10)) for arm in A])
        r[arm] += mu[arm] + np.random.randn()
        n[arm] += 1
        t += 1
    return r, n

def ThS(alpha, T):
    t = 0
    A = [i for i in range(len(mu))]
    n = [0 for i in range(len(mu))]
    r = [0. for i in range(len(mu))]
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sample = [0. for i in range(len(mu))]
while t < T:
    for arm in A:
        mu_hat = (0 + r[arm]) / (n[arm] + alpha**2)
        sigma_hat = alpha / np.sqrt(n[arm] + alpha**2)
        sample[arm] = np.random.normal(loc=mu_hat, scale=sigma_hat)
    arm = np.argmax(sample)
    r[arm] += mu[arm] + np.random.randn()
    n[arm] += 1
    t += 1
return r, n

def SEA_new(alpha, T):
    t = 0
    A = [i for i in range(len(mu))]
    n = [0 for i in range(len(mu))]
    r = [0. for i in range(len(mu))]
    while t < T:
        for arm in A:
            r[arm] += mu[arm] + np.random.randn()
            n[arm] += 1
            t += 1
        if t >= T:
            return r, n

        if len(A) > 1:
            means = np.array([r[arm]/n[arm] for arm in A])
            bonus = np.array([alpha * np.sqrt(T*np.log(T))/n[arm] for arm in A])
            upper = means + bonus
            lower_val = np.max(means - bonus)
            sign = upper > lower_val
            A = [A[i] for i in range(len(A)) if sign[i]]
    return r, n

def UCB_new(alpha, T):
    t = 0
    A = [i for i in range(len(mu))]
    n = [0 for i in range(len(mu))]
    r = [0. for i in range(len(mu))]
    while t < T:
        arm = np.argmax([r[arm]/(n[arm] + 1e-10) + \
            alpha * np.sqrt(T*np.log(T))/(n[arm] + 1e-10) for arm
→in A])
        r[arm] += mu[arm] + np.random.randn()
        n[arm] += 1
        t += 1
    return r, n

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[ ]: T = 500
      N = 5000
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[ ]: sea_old = {}
      ucb_old = {}
      ths = {}
      sea_new = {}
      ucb_new = {}

      eta_list = [0.1, 0.2, 0.4, 0.8]

      for alpha in eta_list:
          print(alpha, end = ' ')

          print("sea_old", end=' ')
          sea_old[alpha] = [SEA(alpha, T)[0] for i in range(N)]
          sea_old[alpha] = np.sum(sea_old[alpha], axis=1)

          print("ucb_old", end=' ')
          ucb_old[alpha] = [UCB(alpha, T)[0] for i in range(N)]
          ucb_old[alpha] = np.sum(ucb_old[alpha], axis=1)

          print("ths", end=' ')
          ths[alpha] = [ThS(alpha, T)[0] for i in range(N)]
          ths[alpha] = np.sum(ths[alpha], axis=1)

          print("sea_new", end=' ')
          sea_new[alpha] = [SEA_new(alpha, T)[0] for i in range(N)]
          sea_new[alpha] = np.sum(sea_new[alpha], axis=1)

          print("ucb_new", end=' ')
          ucb_new[alpha] = [UCB_new(alpha, T)[0] for i in range(N)]
          ucb_new[alpha] = np.sum(ucb_new[alpha], axis=1)

          print("Completed.")
```

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[ ]: policy = [sea_old, ucb_old, ths, sea_new, ucb_new]
      name = ['SE', 'UCB', 'TS', 'SE_new', 'UCB_new']
      i = 0
      for p in policy:
          print(name[i])
          i += 1
          for para in eta_list:
              print(para, np.mean(p[para]))
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[ ]: name = ['SE-', 'UCB-', 'TS-', 'SE_new-', 'UCB_new-']
      fig = plt.figure(figsize=(16, 8))
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```

policy = [sea_old, ucb_old, ths, sea_new, ucb_new]
font = {'size':12}

matplotlib.rc('font', **font)
for i in range(6):
    axx = fig.add_subplot(2, 3, i+1)
    arr = policy[i]
    for alph in [0.1, 0.2, 0.4, 0.8]:
        axx.hist(arr[alph], bins=200, range=(0, 1.02*T), alpha=0.3,
                  label=name[i]+str(alph), density=True)
    axx.legend(prop={'size':12}, loc='upper left')
    axx.set_ylim([0, 0.02])
    axx.get_yaxis().set_ticks([])
plt.subplots_adjust(wspace=0.1)

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