## Checklist

- 1. For all authors...
  - (a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]

In our view both the abstract and introduction accurately reflect the paper as a whole.

(b) Did you describe the limitations of your work? [Yes]

One limitation is that the proposed models are not universal function approximators; see section 3.1. Another limitation is that the linear model seems to outperform the rank-one quadratic model; we do not fully understand this effect, as discussed in the last paragraph of section 4. A third limitation is that models need to be averaged across time to obtain a single, deployable model: see Figure 5. A final limitation is that we do not yet have convergence theorems or regret bounds for the passive-aggressive updates in these models; see the second paragraph of section 5.

(c) Did you discuss any potential negative societal impacts of your work? [Yes]

See the penultimate paragraph of section 5.

(d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [Yes]

The paper conforms to all of the published guidelines. The proposed method is evaluated on a data set that was made publicly available for research and that has not been associated with any personally identifiable or sensitive information.

- 2. If you are including theoretical results...
  - (a) Did you state the full set of assumptions of all theoretical results? [Yes]

The paper contains no proofs, but several calculations. Every attempt was made to state the full set of assumptions behind each calculation (e.g., the footnote on page 5).

(b) Did you include complete proofs of all theoretical results? [Yes]

The calculations should provide enough details to be followed and reproduced by a typical reader. In general where further details might help, the reader is referred to existing papers that provide them; see section 3 before eq. (??). One exception is that we omitted the derivation of eq. (??), which is a tedious (but not difficult) exercise in basic calculus and linear algebra. The paper is intended to be complete without a supplementary appendix.

- 3. If you ran experiments...
  - (a) Did you include the code, data, and instructions needed to reproduce the main experimental results (either in the supplemental material or as a URL)? [Yes]

As part of the supplemental material we have submitted code and instructions to reproduce the main experimental results.

(b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [Yes]

We explained carefully how all models were initialized. The passive-aggressive updates in this paper do not involve learning rates, momentum parameters, or mini-batch sizes. There were no data splits: the models were evaluated in an online manner over an extremely large number (100M) of distinct examples. The averaged models were sampled at regular intervals of 50K training examples.

(c) Did you report error bars (e.g., with respect to the random seed after running experiments multiple times)? [N/A]

We verified that the results on 10M examples were not materially different for five

different values of the random seed; this is reported in section 4. But we were not able to experiment with multiple seeds on the full data set of 100M examples.

(d) Did you include the total amount of compute and the type of resources used (e.g., type of GPUs, internal cluster, or cloud provider)? [Yes]

See the footnote in section ??.

- 4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...
  - (a) If your work uses existing assets, did you cite the creators? [Yes]

The paper cites the researchers [? ? ] that introduced the INFIMNIST and MNIST data sets into the public domain.

(b) Did you mention the license of the assets? [N/A]

These data sets appear to be distributed without a license.

- (c) Did you include any new assets either in the supplemental material or as a URL? [Yes]We include sample code in the supplemental material.
- (d) Did you discuss whether and how consent was obtained from people whose data you're using/curating? [N/A]

The data sets that we use have been in the public domain for a long while.

(e) Did you discuss whether the data you are using/curating contains personally identifiable information or offensive content? [N/A]

## The data does not contain any personally identifiable information or offensive content.

- 5. If you used crowdsourcing or conducted research with human subjects...
  - (a) Did you include the full text of instructions given to participants and screenshots, if applicable? [N/A]

This work did not use crowdsourcing or conduct research with human subjects.

(b) Did you describe any potential participant risks, with links to Institutional Review Board (IRB) approvals, if applicable? [N/A]

This work did not use crowdsourcing or conduct research with human subjects.

(c) Did you include the estimated hourly wage paid to participants and the total amount spent on participant compensation? [N/A]

This work did not use crowdsourcing or conduct research with human subjects.