- We thank all reviewers for their comments. We will correct all typos and address all minor comments in the final paper.
- **Reviewer #1:** Biological plausibility of C1-C3 and ϕ ? C1: Given an input-target pair, C1 means that a model
- makes a prediction from the input, before it learns from the target, which is quite natural for biological neural systems. 3
- C2 and ϕ : C2 is realized by ϕ , and it is very plausible that ϕ can be performed by biological neurons, because some 4
- types of neurons are well-known to respond predominantly to changes in their input [71]. C3: Though it is unnatural 5
- for biological neural systems to have a specific integration step, we show in the supplementary material that relaxing C3
- results in BP with a different learning rate for different layers, which does not violate the core of BP.
- Weight transport problem? In the predictive coding model, the errors are back-propagated by correct weights, because
- the model includes feedback connections that also learn. The weight modification rules for corresponding feedforward 9
- and feedback weights are the same, which ensures that they remain equal if initialized to equal values (see [48]). 10
- Other criticisms for BP (spiking and recurrent neural networks) remain? As discussed in the related work section, they 11
- are left as future work, while this work addresses two of the most crucial ones: local plasticity and autonomy. 12
- Related work of https://arxiv.org/abs/2006.04182? This work was published on 7 Jun 2020 (after the NeurIPS'20 13
- deadline). It includes another approximation to BP but no equivalence; we will add it to the related work. 14
- **Reviewer #2:** Weight transport problem? Please see line 8 in the response to Reviewer #1. 15
- Locality of learning rule? (the update of $\theta_{i,j}^{l+1}$ depends on x_i^l)? According to Eq. 9, the update of $\theta_{i,j}^{l+1}$ actually depends on x_j^{l+1} rather than x_i^l (we suspect the reviewer might have misread Eq. 9), so it is local.
- 17
- Confusion about inference? Alg. 2 explicitly states C1 in the second "Require". In line 158, we make a note that C1 is 18
- omitted in Fig. 2 for simplicity. This note will be included in the caption of Fig. 2. 19
- Full autonomy during the initial convergence of prediction? During the prediction phase, the error nodes change due 20
- to feedforward input, while during learning, the error nodes change due to feedback input. We will clarify that, in order 21
- to prevent learning during prediction, ϕ is equal to 1 only if the change in error node is caused by feedback input. 22
- Reviewer #3: Limitations of PCNs. They are well-discussed in [10,48]; we will add a summary of them. Note that 23
- some limitations have been addressed (e.g., 1-to-1 connections are addressed in [10]). We will also review key studies 24
- illustrating that PCNs are widely used and informative models of information processing in the brain. 25
- Model in [48] already autonomous, because plasticity triggered by network convergence? The plasticity trigger in [48]
- requires global information (i.e., total error in all error nodes), while our trigger ϕ needs only local information, thus, is 27 more plausible for biological implementation. 28
- Experiment of Fa-Z-IL? ϕ with $t_d > 4$ succeeds in all detections (Table 3), i.e., Fa-Z-IL with such ϕ coincides with 29
- Z-IL (BP). We will include the classification results of such Fa-Z-IL, which produces the same results as Z-IL (BP). 30
- Clarification of full autonomy? Fa-Z-IL does require the input to be presented before the teacher to satisfy C1. We 31
- consider this to be a requirement of the learning setup and will make it explicit in the paper, moderating our claim of 32
- autonomy. However, we consider such requirement to be much weaker, compared to switching computational rules
- (BP) and detecting convergence of global variables (IL). We leave the study of removing this requirement or putting it 34
- inside an autonomous neural system as future research. 35
- Moderate the title? We will modify the title to the more specific "Can the Brain Do Backpropagation? Exact 36
- Implementation of Backpropagation in Predictive Coding Networks". 37
- From Z-IL to Fa-Z-IL? We will add the statement that Fa-Z-IL loses formal equivalence to BP, but with $t_d > 4$,
- empirical equivalence always remains. 39
- C1 in [48] should be acknowledged? We will acknowledge this. 40
- Clarification of [48]? In line 42, we have stated that some previous works are equivalent to BP when feedback is 41
- sufficiently weak (i.e., teacher weakly perturbs the network); we will add such clarification when introducing [48]. 42
- Discuss about [46]? We will add a section outlining the differences of learning rules between [46] and Z-IL, along 43
- which we point out that some steps may serve similar general purposes. A deeper study on the connections of the two 44
- substantially different learning rules is left as future research. 45
- Reviewer #4: Moderate the title? Will be changed to "Can the Brain Do Backpropagation? Exact Implementation of Backpropagation in Predictive Coding Networks". 47
- Strong claim? We will moderate the sentence pointed out by the reviewer. 48
- Classification accuracy? The classification accuracy of all situations in Fig. 3 will be added to the final paper: the 49
- averaged accuracies of BP, IL, Z-IL, and Fa-Z-IL are 94.16%, 93.78%, 94.16%, and 94.16%, respectively. 50
- Details of the two criteria? The divergence of the test error is the L1 distance between the corresponding test errors, 51
- averaged over 64 training iterations (the test error is evaluated after each training iteration). The divergence of the final 52
- weights is the sum of the L2 distance between the corresponding weights, after the last training iteration. 53
- Extra description of Fig. 2? Lines 133–141 are the description of Fig. 2; this will be included in the caption of Fig. 2.