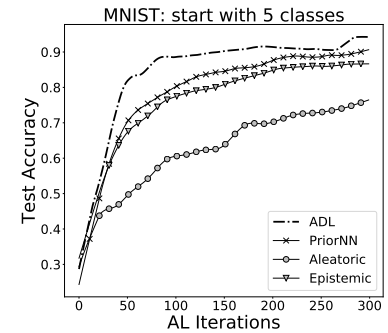


1 We thank all reviewers for their valuable feedback and constructive suggestions. Major comments are addressed below.

2 Reply to Reviewer 1

3 **Q1: Need for an evidence-based subjective logic (SL) framework.** The SL framework provides the theoret-
4 ical underpinning to perform a principled, fine-grained analysis between the 1st-order uncertainty (i.e., pre-
5 dictive entropy as the total uncertainty) and 2nd-order uncertainty (vacuity + dissonance), where evidence
6 plays a central role to unveil the underlying (dynamic) relationship among different uncertainties. Under-
7 standing this dynamic relationship is essential to derive a theoretically sound data sampling process in AL.

8 In particular, Theorem 1 shows the total uncertainty dynamically shifts between
9 high vacuity and high dissonance as more evidence is collected. Guided by this
10 theory, AL can be regarded as an evidence collection process. The evidence-based
11 uncertainties (i.e., vacuity + dissonance) derived under SL, offer a natural way
12 to determine the sources of uncertainty during AL, which starts by focusing
13 on vacuity in early stage when evidence is limited and then gradually shifts
14 to dissonance. Since vacuity and dissonance both depend on evidence, using
15 evidence provides a principled way to trace the dynamic shift between these
16 two sources of uncertainty to best guide data sampling in AL. This is the **key**
17 **advantage** over other types of uncertainty, such as epistemic and aleatoric, which
18 only focus a certain aspect of uncertainty, and their (dynamic) relationship is
19 hard to be precisely quantified as in vacuity and dissonance. Thus, using these
20 uncertainty measures lacks the capability to dynamically adjust the sampling
21 process as the nature and focus of uncertainty change when more data samples



22 are labeled. In sum, while there are various forms of uncertainty measures, the evidence-based (2nd-order) uncertainty,
23 i.e., vacuity + dissonance, offers the most suitable way for active sampling, as justified by our theory and empirical
24 evaluation. The right figure includes additional comparison with other uncertainties: epistemic, aleatoric (Kendall &
25 Gal, 2017), and distributional uncertainty of prior networks (Malinin & Gales, 2018). As can be seen, ADL converges
26 much faster than other uncertainty based sampling functions, which empirically confirms its effectiveness in AL. We
27 will report the comparison results on all other datasets in the revised paper.

28 **Q2: Choice of architecture.** We choose a relatively simple architecture to demonstrate that the good AL performance is
29 due to the sampling function instead of a strong classifier. Several works (eg, [7] and [11]) follow a similar rationale.

30 **Q3: Experiments of a greater scale.** We thank the reviewer for suggesting these large-scale image datasets. Limited by
31 time, we were not able to conduct the experiments on these large datasets and collect the active learning results. An
32 interesting future direction is to combine the architectures suggested by the reviewer and our sampling function and
33 apply to these large datasets.

34 Reply to Reviewer 3

35 **Q1: What “evidence-based entropy” is when claiming entropy can be decomposed into vacuity and dissonance.** Thank
36 you for the suggestion. Entropy decomposition means a high entropy dynamically shifts between a high vacuity and a
37 high dissonance as more evidence is collected, instead of a simple sum of these two uncertainties. We will make this
38 clear in the revised paper.

39 **Q2: Relation to prior work.** The prior networks model (Malinin & Gales, 2018) proposes distributional uncertainty
40 (DU) for OOD detection. While DU can be regarded as a type of epistemic uncertainty that can be used for data
41 sampling in AL, the prior network needs to be properly trained as its parameter must encapsulate knowledge of both
42 in-domain distribution and the decision boundary, making it not very suitable for AL. This is also evidenced by our
43 additional comparison result in Fig. (a). The Noise-Contrastive Priors (Hafner et al. 2018) can also be used for OOD
44 detection as it encourages high uncertainty near the boundary of the training data. However, in the initial phase of AL
45 when the training data is very limited, this measure can be insufficient to explore data samples faraway from the training
46 data. R1 (Q1) offers a deeper discussion on why vacuity + dissonance is more effective for AL than other uncertainties.

47 Reply to Reviewer 4

48 **Q1: Compare to prior networks...ability to capture vacuity.** For comparison with prior networks, please refer to Fig.
49 (a) and R3 (Q2). As the model continues to be trained with AL, it remains uncertainty aware but the total uncertainty
50 (especially vacuity) will decrease. Fig.3 (page 7) shows how vacuity changes along with AL.

51 **Q2: Parameter update and complexity.** ADL is retrained once a labeled sample is added. Time complexity is
52 $O(\text{training_size} \times \text{epoch})$, which is efficient given the small training size in AL.

53 **Q3: Minor note.** DU should be EU; $W = K$ is commonly used for a non-informative prior; it should be $C \rightarrow \infty$; β
54 should be non-negative, which is ensured in our experiments. We will fix these typos.