

1 We appreciate the valuable comments from the reviewers. We will answer reviewers' questions from three aspects, i.e.,  
2 the novelty of the paper, algorithm scalability, and model properties. Due to the page limit, we will also address the  
3 other comments in the paper if accepted.

4 **Novelty:** In respond to *Reviewer 5*, this paper's major novelty is developing a new STL-based learning framework to  
5 enforce multivariate RNN models to follow critical model properties, especially targeting the sequential regression  
6 tasks. Our method creates a practical way to ensure the logic rules' satisfaction in an end-to-end manner. It increases  
7 the robustness of the RNN models. Our approach achieves promising results on real city datasets, i.e., significantly  
8 increasing the satisfaction of model properties (by about four times) and prediction accuracy (by about 18.5%).

9 We have carefully compared our work with all the related papers pointed out by the reviewers. *First*, STL, as a powerful  
10 specification language, has been broadly applied to the specification and verification for CPS applications, such as  
11 robotics [1,2], smart cities, healthcare. Therefore, we also choose STL to express the model properties. STL has been  
12 applied to both continuous and discrete signals. Due to the nature of RNN, the traces in this work are discrete with a  
13 finite length. Using STL to specify CPS properties is not our novelty. However, we systematically identify six critical  
14 types of model properties in CPS, which we believe is valuable for users to define model properties in their context  
15 and utilize our work in practice. *Second*, DNF and many equivalent forms have been used in different contexts. Our  
16 algorithm not only converts STL to DNF, also calculates the satisfaction range for each predicate and thus finds the best  
17 trace closest to a given trace. Besides, we also create algorithms to generate satisfaction traces tailored to deep learning  
18 processes efficiently. *Third*, introducing formal logic to support learning has been a hot topic and achieved promising  
19 performance in recent years, including our work. Most of the current works focus on reinforcement learning [3,4] and  
20 classification tasks [5,6], which have very different scopes than our paper. Their proposed methods do not apply to our  
21 target problem. For example, paper [5] (already cited in our paper) combines first-order logic with neural networks  
22 using a Teacher-Student network structure targeting NLP (classification) tasks. Paper [7] (a paper rejected by ICLR  
23 2020) does apply to RNN models. It adds a term of constraint to the loss function, and tries to reach globally minimal  
24 robustness over the input space. However, it is much more time-consuming and less robust (a soft constraint enforced  
25 by optimization) comparing to our teacher-student network structure. Different from these papers, our work targets  
26 multivariate RNN-based regression tasks, uses a more representative logic for RNN training, and achieves a stronger  
27 satisfaction of the requirement (satisfaction guarantee with the teacher network at the testing time).

28 **Scalability:** In respond to *Reviewer 1*, the computation time of Algorithm 1 is relevant to the number of predicates in  
29 the STL formula. However, we create algorithms to generate satisfaction traces tailored to deep learning processes  
30 efficiently. The time could increase when there are more predicates, but Algorithm 1 only needs to be executed ONCE  
31 in the pre-process (i.e., before the training phase). Therefore, it will not cause any significant delay in training and  
32 testing phases, even for a large amount of data or long-term prediction. Besides, there are approaches to obtaining  
33 a sub-optimal solution in a reasonable time that can be integrated to Algorithm 1 if needed. In our evaluation, the  
34 pre-processing time for all cases (which have reasonable complexity STL formulas as the real-world applications) is  
35 less than 10 seconds. We will also address it in the paper.

36 To briefly answer the other questions from Reviewer 1, (1) the reviewer is right about the teacher network; (2) The  
37 return value is a non-negative real number. If a variable satisfies a constrain in a clause, the term will be evaluated to  
38 0; Otherwise, it will return the minimal distance over all the items in the satisfaction of  $l_i$  (not necessary to be 1). (3)  
39 STLnet is general enough to be applied to transformer-based sequence models. Choosing RNN and its variants is to  
40 show the generalizability of our solution.

41 **Model properties:** In respond to *Reviewer 4*, Model properties broadly exist in real-world applications and systems. In  
42 this paper, we identify several critical types (in Section 2 and evaluation) based on the model properties from existing  
43 papers, systems, and applications in CPS domain. In practice, model properties can be (1) already known by the system  
44 before prediction, e.g., constraints by the physical world, rules followed by the application domains, (2) defined by the  
45 users based on their application (e.g., robotics), (3) mined from the models' historical behaviors. (We also present a  
46 similar discussion at the beginning of Section 2 in the paper.)

47 To briefly answer the other questions from Reviewer 4, (1) RMSE itself cannot capture the temporal correlations of the  
48 sequence like eventually, existence, consecutive changes, etc. (2) [0,24] represents 24 hours in a day. Users can choose  
49 to use () or [] based on if the beginning and ending hours are included. (3) Alg. 1 has a typo that the epsilon set should  
50 be initialized with  $\text{CalculateDNF}(\phi_1, t, \text{sgn})$  where  $t$  is an element of  $T$ .

#### 51 **References:**

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- 53 [2] Dutta, Souradeep, et al. "Learning and verification of feedback control systems using feedforward neural networks." IFAC-PapersOnLine 51.16 (2018): 151-156.
- 54 [3] Li, Xiao, et al. "A formal methods approach to interpretable reinforcement learning for robotic planning." Science Robotics 4.37 (2019).
- 55 [4] Sadigh, Dorsa, et al. "A learning based approach to control synthesis of markov decision processes for linear temporal logic specifications." 53rd IEEE CDC. 2014.
- 56 [5] Hu, Zhiting, et al. "Harnessing deep neural networks with logic rules." arXiv preprint arXiv:1603.06318 (2016).
- 57 [6] Ghosh, Shalini, et al. "Trusted Neural Networks for Safety-Constrained Autonomous Control." arXiv preprint arXiv:1805.07075 (2018).
- 58 [7] Dathathri, Sumanth, et al. "Scalable Neural Learning for Verifiable Consistency with Temporal Specifications." (2019).