

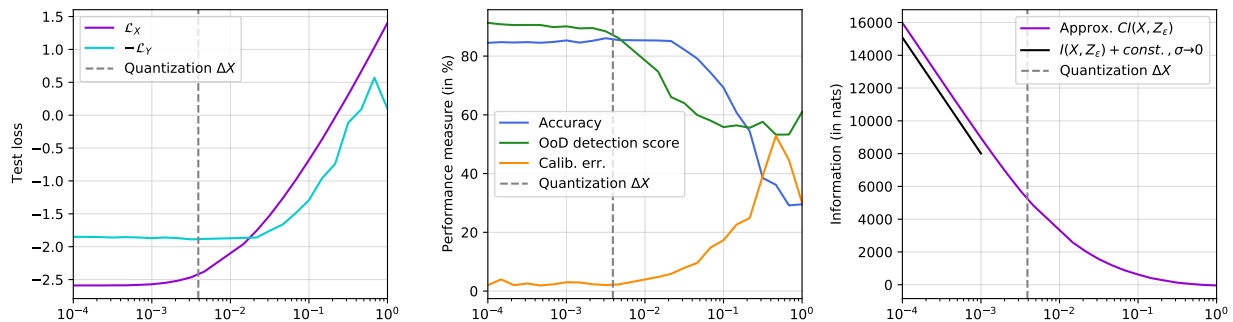
1 We sincerely thank all reviewers for their time and constructive feedback. We will add all minor clarifications and
 2 corrections to the final version (R2, R4, R5), as well as additional generated samples (R1). We are also thankful for the
 3 idea of R1 on how to extend our method using perturbations on Z , and will investigate this in the future. We address the
 4 main questions and criticisms in the following:

5 **$CI(Y, Z)$ as a lower bound (R1).** Thank you for this comment, we realized that we did not mention this in the
 6 paper, even though the answer is straight forward and enlightening: $CI(Y, Z)$ is in fact a lower bound of $I(Y, Z)$.
 7 This can be readily seen from Eq. 6: The first term is the entropy $h(Y)$, because the label distribution $p(Y)$ is known
 8 exactly. The second term can be rewritten as the negative cross-entropy $-h_q(Y | Z)$. For $I(Y, Z)$, we have the
 9 negative entropy $-h(Y | Z)$ as the second term instead. Because $h_q(Y | Z) \geq h(Y | Z)$ (Gibbs' inequality), we have
 10 $CI(Y, Z) \leq I(Y, Z)$. This is essentially the the same as the variational bound originally proposed by Barber & Agakov
 11 (2003): Their Eq. 3 corresponds to our Eq. 6, noting that their x is our Y , and their y is our Z . This is a bound that only
 12 works in this specific case, as the label distribution $p(Y)$ must be known for it to apply. We will add this to the final
 13 version.

14 **Mathematical assumptions about the network g_θ (R4).** We agree that the assumptions should be added to the text
 15 and propositions more explicitly, and we will rectify this for the final version. However, we do not see the assumptions
 16 as a 'fundamental technical difficulty': For all INN architectures used in practice, they are fulfilled by construction.
 17 This includes GLOW, RealNVP, NICE, i-ResNet, and more. In none of these cases, there is any need for any additional
 18 constraints, i.e. the assumptions are fulfilled per default. We refer to works such as Virmaux & Scaman (2018);
 19 Behrmann et al. (2020) for further details.

20 **Strengthening Prop. 1 and properties of CI (R4).** We also think that the CI is of great interest in general and should
 21 be further investigated in future. In our case, it is only used in a very specific way, so we did not consider strengthening
 22 or extending Prop. 1. Instead, we would like to refer to Xu et al. (2020), who derive various further theoretical results
 23 and insights concerning CI in general.

24 **Effect of hyperparameter σ (R5).** In line with this suggestion, we will add some more experiments to the appendix
 25 concerning the effect of σ . As a first step, the following figure shows the behaviour for 25 different models trained with
 26 σ between 10^{-4} and 10^0 (x-axis), and fixed $\gamma = 0.2$. We find that the loss values (left) and performance characteristics
 27 (middle) do not depend on σ below a threshold that is comparable to the quantization step size ΔX . The models
 28 performance does not decrease even when σ is 50 times smaller than ΔX . Detrimental effects might occur more
 29 easily if the quantization steps are larger, e.g. $\Delta X = 1/32$ as used by Kingma & Dhariwal (2018). The rightmost plot
 30 compares our approximation of $CI(X, Z_\epsilon)$ with the asymptotic $I(X, Z_\epsilon) + const.$ for $\sigma \rightarrow 0$, where the constant is
 31 unknown. The slope of the approximation agrees well for small σ , but breaks down for larger values. This, and further
 32 experiments concerning the role of σ will be added to the final version.



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34 References.

- 36 Barber, D. and Agakov, F. V. The im algorithm: a variational approach to information maximization. In *Advances in*
 37 *neural information processing systems*, pp. None, 2003.
- 38 Behrmann, J., Vicol, P., Wang, K.-C., Grosse, R., and Jacobsen, J.-H. Understanding and mitigating exploding inverses
 39 in invertible neural networks. *arXiv preprint arXiv:2006.09347*, 2020.
- 40 Kingma, D. P. and Dhariwal, P. Glow: Generative flow with invertible 1x1 convolutions. In *Advances in neural*
 41 *information processing systems*, pp. 10215–10224, 2018.
- 42 Virmaux, A. and Scaman, K. Lipschitz regularity of deep neural networks: analysis and efficient estimation. In
 43 *Advances in Neural Information Processing Systems*, pp. 3835–3844, 2018.
- 44 Xu, Y., Zhao, S., Song, J., Stewart, R., and Ermon, S. A theory of usable information under computational constraints.
 45 *arXiv preprint arXiv:2002.10689*, 2020.