We thank all reviewers for their comments, and will incorporate suggestions in the final version. Although the goal of 1 this paper is theoretical, we perform experiments to resolve reviewers' concern about practicality of our methods. 2

- Experiment Setup. We compare the proposed algorithms with baseline algorithms on the U.S. 2000 Census Data 3
- containing $n = 5 \times 10^6$ rows and d = 11 columns and UCI YearPredictionMSD dataset which has n = 515, 345 rows 4
- and d = 90 columns. All algorithms are implemented in Python 3.7. To solve the optimization problems induced by 5
- the regression problems and their sketched versions, we invoke the minimize function in scipy.optimize. Each 6
- experiment is repeated for 25 times, and the mean of the loss function value is reported. In all experiments, we vary the 7
- sampling size or embedding dimension from 5d to 20d, and observe their effects on the quality of approximation. 8
- **Experiments on Orlicz norm.** We compare our algorithm in Section 2 with uniform sampling and the embedding 9
- in [2]. We also calculate the optimal solution to verify the approximation ratio. We try Orlicz norms induced by 10
- two different G functions: Huber with c = 0.1 and " $\ell_1 \ell_2$ ". See Table 1 in our submission for definitions. Our 11
- experimental results given below clearly demonstrate the practicality of our algorithm. In both datasets, our algorithm 12 outperforms both baseline algorithms by a significant margin, and achieves the best accuracy in almost all settings.



13 Experiments on symmetric norm. We compare our algorithm in Section 3 (SymSketch) with the optimal solution to 14

verify the approximation ratio. We try two different symmetric norms: top-k norm with k = n/5 and sum-mix of ℓ_1 and 15

- ℓ_2 norm ($||x||_1 + ||x||_2$). See Line 58-60 in our submission for definitions of these norms. As shown below, SymSketch 16 achieves reasonable approximation ratios with moderate embedding dimension. In particular, the algorithm achieves an 17
- approximation ratio of 1.25 when the embedding dimension is only 5d.



(Reviewer #1) Assumption 1. Our sampling algorithm in fact works for ℓ_p norms when p > 2. In general, suppose 19 the function $G: \mathbb{R} \to \mathbb{R}$ satisfies that for all 0 < x < y, $G(y)/G(x) \leq C_G(y/x)^p$, for the Orlicz norm induced by 20 G, given a well-conditioned basis with condition number κ_G , our sampling algorithm returns a matrix with roughly 21 $O((\sqrt{d\kappa_G})^p \cdot d/\varepsilon^2)$ rows such that Theorem 1 holds. However it is not clear how to calculate well-conditioned bases 22 in input-sparsity time when p > 2. Our current method fails since it requires an oblivious subspace with poly(d)23 distortion, and it is known that such embedding does not exist when p > 2 [9]. Since we focus on input-sparsity time 24 algorithms in this paper, we did not include the p > 2 case. We will add more discussion on this in the final version. 25

(Reviewer #2) Results on symmetric norm. We disagree that this is an incremental improvement. First, the previous 26 embedding with $d \log n$ distortion only works for Orlicz norms, and in this paper we give the first subspace embedding 27 28 for general symmetric norms. Second, the construction in [7] is only for streaming algorithms. To construct a subspace embedding, we need to show that (i) norms of all vectors in a subspace are preserved and (ii) there is a simple estimator 29

- in the sketch space. Neither of them can be satisfied by the construction in [7]. 30
- Comparison with [11]. First, our definitions for Orlicz norm leverage score and well-conditioned basis, as given in 31 Definition 2 and 3, are different from all previous works and are closely related to the Orlicz norm under consideration. 32
- 33
- The algorithm in [11], on the other hand, simply uses ℓ_p leverage scores. Under our definition, we can prove that the sum of leverage scores is bounded by $O(C_G d\kappa_G^2)$ (Lemma 4), whose proof requires a novel probabilistic argument. In 34
- contrast, the upper bound on sum of leverage scores in [11] is $O(\sqrt{nd})$ (Lemma 38 in [11]). Thus, the algorithm in 35
- [11] runs in an iterative manner since in each round the algorithm can merely reduce the dimension from n to $O(\sqrt{nd})$. 36
- while our algorithm is one-shot. We will of course add a more detailed comparison with [11] in the final version. 37
- (Reviewer #3) The uniqueness of α follows from the assumption that G is strictly increasing, in which case the two 38
- definitions are equivalent. The assumption that G is strictly increasing was also implicitly made in Andoni et al. [2]. 39
- It is indeed an interesting problem to generalize our techniques to other problems, e.g., classification problems and 40 non-linear regression problems. We leave this as a future work. 41