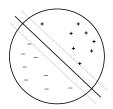
# Algorithms and hardness results for parallel large-margin learning

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#### Setting:

- Target:  $\gamma$ -separated halfspace
- Domain: unit ball in R<sup>n</sup>



- Computational model: PRAM (parallel RAM)
- Question: can output an  $\epsilon$ -accurate hypothesis using
  - poly  $\left(\log n, \log \frac{1}{\gamma}, \log \frac{1}{\epsilon}\right)$  time
  - poly  $\left(n, \frac{1}{\gamma}, \frac{1}{\epsilon}\right)$  processors?

#### Positive result

Dependence on  $1/\epsilon$  already handled by Boost-by-majority [Fre95]. Revised goal:

- poly  $\left(\log n, \log \frac{1}{\gamma}\right)$  time
- poly  $\left(n, \frac{1}{\gamma}\right)$  processors.

Algorithm	Number of processors	Running time
Perceptron	$\operatorname{poly}(n,1/\gamma)$	$\tilde{O}(1/\gamma^2)(\log n)$
SmoothBoost	$\operatorname{poly}(n,1/\gamma)$	$\tilde{O}(1/\gamma^2)(\log n)$
LP	1	$\operatorname{poly}(n, \log(1/\gamma))$
This paper	$\operatorname{poly}(n,1/\gamma)$	$\tilde{O}(1/\gamma) + O(\log n)$

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### Algorithm

- Parallel boost-by-majority to handle  $\epsilon$ -dependence [Fre95]
- · Weak learner:
  - Random projection [JL84,AV99]
  - Interior point method [Ren88]
    - Invert Hessian using parallel matrix inversion [Rei95]
    - Round intermediate solutions (preserve margin)

## Negative result



- Some boosters [KM95,MM00,KS02,LS05,LS08] use decision trees or branching programs.
- Calls to weak learners from the same "layer" parallelizable.
- Q: Can save iterations?
- A: No (so  $\Omega(1/\gamma^2)$  iterations needed)
- · Proof sketch:
  - · variables conditionally independent given label
  - in stage *i*, give variable *i* to all weak learners.