

1 We agree with R3 and R4’s suggestion to expand our discussion of motivation and use-cases for determinantal point  
2 processes (DPP) as a tool in machine learning (ML). In the camera ready version we will stress and clarify that DPP  
3 sampling is already a well established tool in the field of ML.

4 DPP sampling has found applications in core ML problems such as stochastic optimization [20], data summarization  
5 [3], Gaussian processes [2], recommender systems [11], and many more. Its effectiveness has been verified repeatedly  
6 at top ML venues. Including only recent years (due to space), it has seen success at ICML’16 [14], ICML’17 [9, 12, 19],  
7 ICML’18 [3] and ICML’19 [2, 7, 10, 18], UAI’17 [20], AAAI’17 [8] and AAAI’19 [21], NeurIPS’16 [13, 15, 17],  
8 NeurIPS’17 [5, 16], NeurIPS’18 [1, 4, 6, 11], and even more successful applications of DPP sampling are likely to be  
9 present in NeurIPS’19.

10 We will also clarify how our approach directly impacts all of these applications. Brief summary: First, we rigorously  
11 *proved* that the samples returned by DPP-VFX are distributed *exactly* as defined by the DPP distribution. Therefore,  
12 from a black-box point of view (i.e., the point of view of the applications mentioned), samples drawn from a DPP or  
13 returned from DPP-VFX are indistinguishable, and retain the effectiveness highlighted in the literature [2, 3, 11, 20].

14 As demonstrated in the paper both theoretically and empirically, our method of implementing this black box provides  
15 a *significant* speed-up over existing approaches (often by many orders of magnitude), to the point where it makes  
16 large-scale application of DPPs feasible when previously it was not.

17 We will also address the concerns shared by R1 and R3 regarding the colors of the graphs (thanks for catching that!).

18 We also thank R4 for the references on Poisson Disk sampling, we will include them in the discussion of existing works.

### 19 Addressing specific comments from Reviewer 3

20 *“It is claimed that [...] but it is not clear that this paper is relevant for our field.”*

21 We strongly disagree with this remark, because

- 22 1. the relevance of black-box DPP samplers to ML is established by a large body of research (see above), an ICML’19  
23 workshop and a NeurIPS’18 tutorial, and
- 24 2. we provide an *exact* DPP sampler that is orders of magnitude faster than the state-of-the-art.

25 *“Can you do computational cross-validation experiments to measure the test error of your algo  
26 versus other baselines?”*

27 The empirical accuracy and effectiveness of DPP sampling is well established for many ML tasks (again, see the  
28 references above). Our algorithm, DPP-VFX, is simply a *very fast and exact implementation* of a DPP sampler.  
29 Therefore it would output the same samples as the other exact DPP sampler baselines but faster.

30 *“Also is there some metric (other than test error) for measuring the empirical accuracy of your  
31 sampling algo, relative to baselines?”*

32 The most appropriate metrics to evaluate for DPP-VFX is sampling speed, and we rigorously validated it empirically,  
33 showing that it significantly outperforms state-of-the-art baselines. Note that previous *approximate* sampling methods  
34 also had another metric to validate, i.e. they had to empirically show that their samples were close enough to a DPP  
35 distribution. However we *prove* that DPP-VFX’s samples are distributed *exactly* according to the DPP, and do not need  
36 to measure this metric empirically, since any negative empirical results would just be due to experimental error.

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