

1 Thank you to the reviewers for the constructive and positive comments. Many comments had to do with positioning
2 relative to existing work, which we will clarify in a revision. The comments can be broken into two groups: point
3 estimation methods and Bayesian methods.

4 **Point Estimation**

5 We chose to investigate the ability of methods to produce calibrated posteriors, but agree that evaluation of point
6 estimates is an interesting and important question. Our initial hypothesis was that noise-aware methods will in general
7 perform similarly to their noise-naive counterparts for point estimation. We observed this in preliminary experiments
8 for simple estimation problems (not regression). However, in ongoing applications of our method from this paper, we
9 observe that it produces better point estimates than noise-naive SSP. Furthermore, noise-naive SSP is a competitive and
10 often state-of-the-art baseline for point estimation (Foulds 2016, Wang 2018). We therefore plan on exploring this more
11 deeply in the future.

12 In general, a Bayesian method is not expected to produce better point estimates than a non-Bayesian counterpart unless
13 the prior is informative.

14 We also conjecture that noise-aware inference will almost never hurt when it comes to point estimation, when compared
15 to a similar noise-naive algorithm. We also conjecture that it will not help *in general*, which is confirmed by experiments
16 in simple estimation problems. However, there are two possible mechanisms by which noise-aware inference *can*
17 improve point estimation. One is by automatically respecting any constraints on parameters, if present. Another is
18 by avoiding certain pathologies of noise-naive methods. For example, for linear regression, noisy sufficient statistics
19 introduce bias into the traditional least-squares estimator, which is unbiased in the absence of noise introduced for
20 privacy. Our noise-naive Bayesian method may avoid this pathology.

21 **Other Bayesian Methods**

22 As for other Bayesian methods, all are noise-naive. We compared to naive SSP, which we consider to be the most
23 competitive baseline in this setting. The posterior sampling MCMC method due to Wang (ICML 2015) allows public
24 release of many posterior samples (unlike OPS), but still suffers from per-sample privacy loss due to the noise injected
25 in each iteration. Private variational inference (VI) is most relevant for problems where the original posterior inference
26 problem requires VI, i.e., when naive SSP is not an option. Bayesian linear regression permits conjugate updates and
27 therefore we can use naive SSP. In fact, VIPS due to Park et al. uses naive SSP on a per iteration basis within the
28 variational inference framework. It is clearly better to privatize the full sufficient statistics only once as in naive SSP.
29 We will clarify these points in the related work section.

30 **Runtime and Data Size**

31 There are two parameters that may affect runtime: number of individuals and number of dimensions. The plot in Figure
32 3f addresses the former. Its purpose is to emphasize that the runtime of MCMC-Ind scales with the number of individuals,
33 but the runtime of Gibbs-SS methods do not, due to their usage of fixed-dimension sufficient statistics. We will clarify
34 that point in the text. The main purpose of the plot was not to compare against Naive or to make a statement about
35 runtime for specific practical settings, though that is a question of interest.

36 While we have not run in-depth experiments on running time relative to covariate dimensionality, we can understand
37 its effect analytically. Let d be the covariate dimension. The most expensive operation used by Gibbs-SS will be the
38 inversion of the covariance matrix (defined in Equation 3) in the NormProduct subroutine on Line 4 of Algorithm 1.
39 This matrix has dimension $(d^2 + d + 1) \times (d^2 + d + 1)$, where $d^2 + d + 1$ are the total number of components in the
40 feature function vector $t(\mathbf{x}, y) = [\mathbf{x}\mathbf{x}^T, \mathbf{x}y, y^2]$. The cubic matrix inversion would then be $O((d^2 + d + 1)^3) = O(d^6)$.
41 Modern computing platforms can reasonably invert matrices of size 10K or more, corresponding to linear regression
42 with $d \approx 100$ features.

43 **Misc.**

44 We agree with R1's suggestion to cite McSherry & Mironov's KDD'09 paper as an early work on SSP.

45 R1 correctly notes that the normalization of the X and y data in the Section 4.3 case study is in fact not a private
46 operation and the normalization constant would have to be publicly released in order to make predictions on new
47 instances. We found this step to be a preprocessing assumption prevalent in many existing works, e.g. the Jalko et
48 al. paper previously mentioned by R3, and one could assume these bounds come from domain knowledge instead of
49 sensitive private data.