

1 We wish to express our appreciation to the reviewers for their insightful comments on our paper. In what follows, we
2 will answer every comment from each reviewer. All responses are reflected in our camera-ready version.

3 ■ Reviewer #1

4 > **It is better to add a section: comparison with related works, to highlight the main contributions.**

5 Thank you for the proposal. We will add a section for comparison to DRS or more sophisticated Metropolis-Hasitings
6 GAN focusing on the difference between their rejection sampling-based scheme and our OT-based method.

7 ■ Reviewer #2

8 > **Firstly, the quality of the writing leaves a lot to be desired for a conference such as NeurIPS. ... Secondly, I
9 felt that clarity is lacking in many places. ...**

10 We are sorry for that our writing makes itself hard to follow. As reviewer #2 commented, we believe fixing it will im-
11 prove our paper, so we will reconsider expressions from grammatical standpoint and logical viewpoint in our revise.

12 > **More concretely, in section 2.3, Theorem 1 is stated. ... Line 25 in supplementary material (pertaining to
13 equation (7)): "... What is an automorphism, and what is the basis of assumption (7). To me, it looks like
14 something relating to a Monge Problem description, but I see no connection here.**

15 Thank you for the important comment. Yes, the automorphism T we assume in Theorem 1 is the solution of cor-
16 responding Monge problem. We will emphasize it in our revise and explain the basis of the assumption along the
17 following reasoning. As commented by reviewer #3 (line 35), there is a subtle issue on uniqueness in the Monge
18 problem because of the norm $\|x - y\|_2$ that is not strictly convex. So, we need the assumption in Theorem 1 to make it
19 mathematically accurate because we cannot avoid using the existence of a solution in our proof. In our opinion, a proof
20 with another milder assumption would be too technical and out of purpose in this paper. Instead of it, let us explain
21 why the assumption is reasonable. One known method [1] to find a solution is based on relaxing the cost to strictly
22 convex cost $\|x - y\|_2^{1+\epsilon}$ with $\epsilon > 0$. Within the strictly convex cost, the unique solution exists [2]. So one can get an
23 original solution by taking limit $\epsilon \rightarrow 0$. Interestingly, their construction, $T^{(\epsilon)}(y) = \min_x \{\|x - y\|_2^{1+\epsilon} - D^*(x)\}$, is
24 almost same as ours, $T(y) = \min_x \{\|x - y\|_2 - D^*(x)\}$. In addition to it, DOT works only when $\|x - y\|_2$ is small
25 enough for given y in our experiments. In this case, there is no big difference between $\|x - y\|_2$ and $\|x - y\|_2^{1+\epsilon}$, and
26 it suggests our T approximates their $T^{(\epsilon)}$. All these encourage to introduce the assumption in Theorem 1.

27 > **A third, ... e.g equation (15) in the supplement, and equation (17) in the main paper. I believe this expression
28 might be missing a negative sign. ... In equation (15), the variable upon which integration is performed (dy) has
29 a negative sign in the delta function, suggesting that we need a negative sign. Please clarify.**

30 Thank you for careful reading. We think there is no need for a negative sign because the delta function is “even
31 function”, i.e. $\delta(-x) = \delta(x)$. Rigorously speaking, it should be treated as measure and is positive by definition.

32 [1] L. Caffarelli, M. Feldman, and R. McCann. *Journal of the American Mathematical Society*, 15(1):1–26, 2002.

33 [2] W. Gangbo and R. McCann. *Acta Mathematica*, 177(2):113–161, 1996.

34 ■ Reviewer #3

35 > **The proof demonstrates that $T(y)$ is a minimizer of the right hand side of the equation, but it does not show
36 uniqueness. In fact, it is easy to construct examples ... Could the authors please comment on this and also
37 comment if this is an issue that was encountered during the experiments.**

38 Thank you for the important comment. It is related to reviewer #2’s comment (line 12). We agree there is an issue on
39 uniqueness in general, like reviewer #3’s example. But, there is a natural way to get a solution provided in [1] (line
40 32). They first relaxed the problem to $\|x - y\|_2^{1+\epsilon}$ by small $\epsilon > 0$, then constructed the minimizer $T^{(\epsilon)}$ (s_ϵ in their
41 paper, defined in line 23 in this manuscript) in essentially the same way as our derivation. $T^{(\epsilon)}$ is uniquely defined
42 thanks to strictly convex nature of the relaxed cost function [2] (line 33). After that, they took $\epsilon \rightarrow 0$ limit to get the
43 solution. This approach is quite similar to DOT approach because $T^{(\epsilon)}$ with infinitesimally small ϵ is almost same as
44 T in our paper by construction. Just in case, we assumed that there exists a certain map T in Theorem 1 to make our
45 proof mathematically correct. In fact, we have not encountered any issue on experiments except for how to choose
46 learning rate in gradient descent DOT. And it was also discussed in lines 105~122 in the supplementary material.

47 > **How does the increase in runtime of the proposed algorithm compare to using a more powerful architecture?
48 We just used gradient of G and D , so it scales same as the backprop. For reference, we put down real runtimes here.**

49 Tesla P100:

Swissroll (WGAN-GP)	CIFAR-10 (SN-DCGAN)	STL-10 (SN-DCGAN)	ImageNet (SN-ResNet)
0.310(02)s/30 updates	1.04(01)s/30 updates	1.05(01)s/30 updates	2.52(01)s/30 updates

50 The error is estimated by 1std on 10 independent runs. We will add theoretical runtime and list of the real runtimes.

51 > **I would have preferred the authors to use faithful reimplementations of existing architectures ... The section
52 on the experiments on ImageNet should be expanded over the CIFAR-10 section.**

53 We sorry for insufficient writing, but our models are based on architectures from the relevant publications, mainly
54 based on SNGAN paper [7] in the reference of the supplementary material. We will cite it appropriately. On the
55 ImageNet experiment, we will explain more including detail of the architectures. Thank you for the comment.