

1 We thank all the reviewers and the AC for their time, effort and constructive feedback. [W1], [W2] and [W3] are
2 references included in this response.

3 **R1, R2, R3: Suitability of numerical experiments.** We appreciate the concern of all reviewers with respect to the
4 numerical simulations. We would like to note that (i) this is mainly a theoretical paper that proves properties of the
5 GST (as R3 remarked) and that (ii) the Diffusion GST is very similar to the method in [W1] which has been compared
6 extensively with other methods (as R1 observed), and therefore we expect similar numerical results as those in [W1]. In
7 any case, we understand, and share, the concerns of the reviewers, so we propose the following changes to the numerical
8 section. First, we will include an explicit comparison with the GST of [W1]. This method will replace the diffusion
9 scattering, since both are very similar (the only differences being the use of the lazy random walk matrix instead of the
10 lazy adjacency matrix, and the use of moments beyond the mean for the low-pass operator ϕ). Second, we will include
11 comparison with a trainable GIN in [W2], in terms of stability of the resulting architectures. We note that comparing
12 performance with trainable GNNs is tricky since it is highly dependent on the size of the available training set and
13 the details of the training stage (number of epochs, learning rate, etc.), which do not occur in GSTs (which are not
14 trainable). Third, we will add clarification and proper links to the Facebook graph [35] and the authorship attribution
15 dataset [36, W3], to emphasize that these are publicly available, while explaining that we are concerned with datasets
16 involving graph signals, since we want to show how changes in the underlying topology affect the processing of the
17 same signals (i.e. datasets involving graph classification, as those in [W1], where changing the underlying graph changes
18 the graph signal are not useful to illustrate Theorem 1 –even though, in practice, they work–). Fourth, as suggested
19 by R1, we will add a clarification and give due credit to the very good work of [W1] to refer to a more exhaustive
20 comparison between GSTs and other state-of-the-art methods. We hope that these changes will address the concerns of
21 the reviewers. **R1: Structural constraint and recovery of Mallat’s scattering result.** The structural constraint allows for
22 edge weights dilations or contractions (i.e. all edge weights increase or all edge weights decrease, albeit with different
23 relative changes). This is required to control the impact that topology changes have on the eigenvectors. Changes
24 such as adding or dropping edges incur in a constant value $\varepsilon = \mathcal{O}(1)$, and as such fix a nonzero minimum for the
25 upper bound. In the very limited number of cases when a topology change can be exactly pinpointed to a change in the
26 eigenvectors, the results in this paper can be improved. One such case is that of the line graph, where it is known how
27 the eigenvectors change when dilating and contracting the edge weights (the effect of a diffeomorphism in [10]), and
28 thus recovering the result in [10]. As space allows, the first observations will be added before Remark 2, while the
29 latter observation will be moved from Remark 1 to a new paragraph and expanded. If necessary, further clarifications
30 on these relationships will be discussed in the supplementary material. **R1: Graph similarity measures.** We would
31 like to clarify that the task is not to compare graph structures in terms of their extracted features, but to analyze how
32 features extracted from graph signals change when the underlying support changes (either because it changes with
33 time, or because it is unknown and has to be estimated, among other examples). The measure of similarity we use in
34 this work is reminiscent of the Gromov-Hausdorff distance, albeit using the spectral norm of the GSO, instead of a
35 max-norm. The comparison with Weisfeller-Lehmann test will hopefully be taken into account by the inclusion of the
36 GIN [W2] in the numerical experiments. **R3: Relation to other GNNs.** Most existing GNNs (with the notable exception
37 of GATs) regularize the linear transform of traditional neural networks by using a graph convolution (5). In this respect,
38 the main computational core of doing a graph convolution followed by pointwise nonlinearities, is the same in GSTs
39 than in GNNs. The main exception, though, is that while GNNs learn the filter coefficients h_k (through different
40 parameterizations), GSTs design them using graph wavelets. Likewise, since Prop. 2 shows stability of the graph
41 filters, which are the same as for GNNs, our stability results may be extended to GNNs with appropriate regularization
42 (since trainable parameters will appear in the bound constants) which is the subject of ongoing work. **R3: Prop. 3.**
43 The formal assumption in Prop. 3 indicates that all involved graph filters in the multiresolution wavelet bank have to
44 satisfy the integral Lipschitz continuity. However, this can be inherited directly from the mother wavelet satisfying
45 the requirement. The hypothesis in Prop. 3 will be changed to reflect this. **R3: Theorem 1.** The bound in Theorem 1
46 depends on difference between the graphs as defined in (16). This difference will certainly depend on the particularities
47 of the graph topologies considered. Theorem 1 states that it does not depend on the spectral norm of the graph. This
48 will be clarified after (19). **R3: Different number of nodes.** As the theorem is stated now, it requires that both graphs
49 have the same number of nodes. The case when they do not, can be addressed by using correspondences in the same
50 manner as Gromov-Hausdorff distance. This case is beyond the scope of this paper and is currently ongoing work. **R2:**
51 **Computation of bound in Fig. 2.** The bound in Fig. 2 is computed as in (19). The values of all the constants involved
52 are explained in the supplementary material due to lack of space. In any case, we will add a specific clarification
53 pointing out to this fact in the revised version. **R3: Update of literature review.** We thank the reviewer for bringing to
54 our attention this recently published papers. They will be added to the introduction, and discussed.

55 [W1] F. Gao, G. Wolf, and M. Hirn, “Geometric scattering for graph data analysis”, in *ICML 2019*.

56 [W2] K. Xu, W. Hu, J. Leskovec, and S. Jegelka, “How powerful are graph neural networks?” in *ICLR 2019*.

57 [W3] E. Isufi, F. Gama, and A. Ribeiro, “Generalizing Graph Convolutional Neural Networks with Edge-Variant Recursions on
58 Graphs,” in *EUSIPCO 2019*.