

1 Thanks to all reviewers for their motivating comments. We appreciate the deep insights of the
2 reviewers and their constructive suggestions which helped a lot to improve the paper.

3 **Overall: [new figure and animations → R1 10] & R2 2.1, 2.2, 5.1]:** We include a figure similar
4 to Fig.2 for Atari game Venture and animations that show reward redistributions during the games.

5 **[analyzing Atari results → R2 2.1, 2.2, 2.3, 5.1 & R3 failure]:** For Atari games, we investigated
6 failures and successes of RUDDER. We discuss those in the new version. RUDDER failures (LSTM
7 problems): Breakout (slow learning), DoubleDunk (explaining away), Hero (spurious redistributed
8 rewards), Qbert (overfits to first levels), MontezumaRevenge (exploration problem). RUDDER
9 successes (redistributed rewards): Frostbite (moving to igloo), Seaquest (getting oxygen), Venture
10 (moving to treasure), Phoenix (shooting at boss shield).

11 **[immediate reward experiment → R3]:** In grid worlds where the agent has to move to a target, no
12 reward was redistributed with Q -value differences as immediate reward. In probabilistic environments
13 the reward was larger near the target. For delayed reward, positive (negative) rewards are redistributed
14 to steps toward (away from) the target. Rewards are redistributed to changes in reward expectations.
15 For example, losing a queen in the game chess receives negative redistributed reward.

16 **[heavy code → R3]:** A lightweight RUDDER code for the tabular case (Q -table) was already
17 included in the submission. We extended this code to PPO and used it for additional experiments on
18 Artificial Task (III). All code will be in a github repository.

19 **[motivation contribution analysis → R3]:** We placed the motivation of contribution analysis in the
20 appendix (lines 1506-1514). We now also do it in the main paper. Sensitivity analysis determines how
21 infinitesimal changes of the input lead to infinitesimal changes at the output. We are not interested in
22 infinitesimal changes of actions or inputs but in large changes. In [1] disadvantages of sensitivity
23 analysis are pointed out, which are more severe for reward redistribution and lead to spurious rewards.

24 **R1: [6] and 9) RUDDER and GAE]:** GAE fits perfectly with RUDDER. For optimal reward
25 redistribution GAE is justified by Theorem 3, which states that the advantage function does not
26 change. For non-optimal reward redistribution, GAE redistributes the reward further back.

27 **[7] and 9) GAE baseline]:** For Atari, both RUDDER and the baseline already use GAE based on the
28 OpenAI PPO implementation. We now move the introduction of GAE [2] and TRPO [3] to the main
29 paper. We performed additional experiments on Artificial Task (III) but with function approximation
30 to compare PPO+GAE, RUDDER-PPO, and RUDDER-PPO+GAE. Again RUDDER is exponentially
31 faster than PPO+GAE. RUDDER-PPO+GAE is slightly better than RUDDER-PPO. We report these
32 experiments in the new version.

33 **[10] Fig.2]:** Thanks, we will improve the figure accordingly.

34 **[11] advantage and future zero reward]:** For optimal reward redistribution, learning the advantage
35 function a^π is simplified to estimating the mean of immediate rewards: $a^\pi(s_t, a_t) = r(s_t, a_t) -$
36 $\sum_a \pi(a | s_t) r(s_t, a)$. Consequently, the response function $\chi(l; s_t, a_t)$ is zero except for $l = 0$. The
37 future expected reward can be expressed as $\kappa = \mathbb{E}[A_t - R_{t+1} + v(s_t) | s_t, a_t]$. For GAE(γ, λ), λ
38 determines to what extend the value function replaces the sum of future rewards in A_t . $\lambda = 0$ gives
39 $\kappa = \gamma \mathbb{E}[v(s_{t+1}) | s_t, a_t]$, while $\lambda = 1$ gives $\kappa = \gamma \mathbb{E}[\sum_{l=0}^{\infty} \gamma^l R_{t+l+2} | s_t, a_t]$.

40 **R2:** The interpretation, visualization, and analysis of the Atari games is of general interest, therefore
41 we answered them in "Overall" above.

42 **[RUDDER limitations]:** We will mention that RUDDER is not effective without delayed rewards
43 since LSTM learning takes extra time and has problems with very long sequences. Furthermore,
44 reward redistribution may introduce disturbing spurious reward signals.

45 **R3: [bias-variance analysis]:** Absolutely. We will try to elaborate more on the topic.

46 **[Fig. S6]:** Probably space limits will not allow this.

47 **[Q1 off-policy]:** The lessons buffer is only used for LSTM training (reward redistribution) but not for
48 PPO learning. PPO learning is justified with any reward redistribution but if it is on-policy, learning
49 is more efficient. Still, off-policy lessons buffers are not critical since they contain episodes with
50 low and high reward. Low reward is less dependent on the policy. High reward episodes are biased
51 towards the current policy since it has learned to produce them.

52 **[Q2 TD bias/ MC variance]:** The estimates are unbiased if the future expected rewards are set to
53 zero like for direct Q -value estimation. The variance of MC is in general smaller even if reward
54 redistribution introduces variance.

55 **[Tab. S6]:** Sorry. We corrected the wrongly placed table headings.

56 **[C1 not defined terms], [C2 merging para.], [C3 Eq.(2) in Th. 3]:** Done, thanks!

57 **[ensure not to fail]:** It is not obvious to us how to ensure that RUDDER improves the baseline.

58 Thank you very much for the encouraging words. Especially as we worked hard and for a long time
59 on this project, this is very rewarding.

- 60 [1] G. Montavon et al. Methods for interpreting and understanding DNNs. *Digit Signal Process*, 73:1–15, 2017.
61 [2] J. Schulman et al. High-dim. continuous control using generalized advantage estimation. *ArXiv*, 2015.
62 [3] J. Schulman et al. Trust region policy optimization. *ArXiv*, 2015.