DAMEX: Dataset-aware Mixture-of-Experts for visual understanding of mixture-of-datasets

Supplementary Material

Anonymous Author(s) Affiliation Address email

This document provides detailed derivation for the convergence behaviour of vanilla MoE on mixture of-datasets.

Mixing datasets in Vanilla MoE does not guarantee convergence with fixed number of experts

In the main paper, we empirically show the benefits of using our proposed DAMEX against vanilla
MoE when mixing multiple datasets. Here we provide theoretical evidence that vanilla MoE do not

7 guarantee convergence when mixing multiple datasets. Hence motivating the need for our method.

8 **Problem formulation.** Consider a binary classification problem over *P*-patch inputs where each 9 patch has *d* dimensions and label $y = \{\pm 1\}$. Thus, a labeled data point (\mathbf{x}, y) has input $\mathbf{x} =$ 10 $(\mathbf{x}^{(1)}, \mathbf{x}^{(2)}, \mathbf{x}^{(3)}, \dots, \mathbf{x}^{(P)}) \in (\mathbb{R}^d)^P$ is a collection of P patch inputs with *y* as the data label. The 11 data \mathbf{x} is generated from *K* clusters.

12 Chen et al. [2022] proves that in such a binary-classification problem, an MoE layer converges to an 13 o(1) test loss and zero training loss. Since, such a classification problem has an intrinsic clustering 14 structure that may be utilized to achieve better performance. Examples can be divided into K clusters 15 $\bigcup_{k \in [K]} \Omega_k$ based on the distance from the cluster-center: an example $(\mathbf{x}, y) \in \Omega_k$ if and only if at 16 least one patch of x aligns with cluster Ω_k .

Specifically, Chen et al. [2022] Lemma 5.2 states that with data $\mathbf{x} \in (\mathcal{R}^d)^P$ the expert $m \in M_k$ can achieve nearly zero test error on the cluster Ω_k but high test error on other clusters $\Omega_{k'}, k' \neq k$.

19 We will extend their formulation to multiple datasets x_1 and x_2 drawn from similar distribution.

Lemma 1: A mixture of two datasets $\mathbf{x} = \mathbf{x}_1 \cup \mathbf{x}_2$, does not always results in the convergence of a MoE layer, such that an expert $m \in [M]$ achieve nearly zero test error on cluster Ω_{k_1} and Ω_{k_2} but high test error on all other clusters in both distributions $\Omega_{k'_1}, k'_1 \neq k_1$ and $\Omega_{k'_2}, k'_2 \neq k_2$.

Proof: We will prove this by contradiction. Assume that we choose a K, such that VC dimension of [M] experts is equal to K. Since, $\mathbf{x}_2 \neq \mathbf{x}_1$, the VC dimension of a model required to learn both $\mathbf{x}_1 \cup \mathbf{x}_2$ is at least K + 1. But, our [M] experts cannot converge for more than K VC dimension. Contradiction.

- 27 Thus, we show that vanilla MoE does not guarantee convergence with mixture of datasets. However,
- if we divide the dataset-expert pair using the proposed DAMEX approach then we can ensure that
- each expert attends to a separate input data distribution x leading to better convergence.

References

- Zixiang Chen, Yihe Deng, Yue Wu, Quanquan Gu, and Yuanzhi Li. Towards understanding mixture of experts in deep learning. *arXiv preprint arXiv:2208.02813*, 2022.