
Supplementary Materials: *SimMTM: A Simple Pre-Training Framework for Masked Time-Series Modeling*

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1 A Implementation Details

2 All the experiments are repeated five times, implemented in PyTorch [12] and conducted on NVIDIA
3 A100 SXM4 40GB GPU. We implement the baselines based on their official implementation and
4 follow the configuration from their original papers. For the metrics, we adopt the mean square error
5 (MSE) and mean absolute error (MAE) for the time series forecasting. As for the classification,
6 accuracy, precision, recall, F1 score, and their average value are recorded.

7 A.1 Dataset Description

8 We conduct experiments to evaluate the effect of our method under in-domain and cross-domain
9 settings on twelve real-world datasets for two typical time series analysis tasks: forecasting and
10 classification, covering diverse application scenarios (electricity system, neurological healthcare,
11 human activity recognition, mechanical fault detection, and physical status monitoring), different
12 types of signals (ECG, EMG, acceleration, vibration, power load, weather, and transportation),
13 multivariate channel dimensions (from 1 to 862), varying times series lengths (from 96 to 5120) and
14 large span sampling ratio (from 100 Hz to 4000 Hz). The detailed descriptions of these datasets are
15 summarized in Table 1.

16 (1) **ETT (4 subsets)** [26] contains the time series of oil temperature and power load collected by
17 electricity transformers from July 2016 to July 2018. ETT is a group of four subsets with different
18 recorded frequencies: ETTh1/ETTh2 are recorded every hour, and ETTm1/ETTM2 are recorded
19 every 15 minutes.

20 (2) **WEATHER** [18] includes meteorological time series with 21 weather indicators collected every
21 10 minutes from the Weather Station of the Max Planck Biogeochemistry Institute in 2020.

22 (3) **ELECTRICITY** [15] records the hourly electricity consumption of 321 clients from 2012 to
23 2014. Values are in kW of each 15 min. All time labels report to Portuguese hour. However, all days
24 present 96 measures (24×4). For every year in March, time change day (which has only 23 hours),
25 values between 1:00 am and 2:00 am are zero for all points. For every year in October, time change
26 day (which has 25 hours), the values between 1:00 am and 2:00 am aggregated consumption of two
27 hours.

28 (4) **TRAFFIC** [13] encompasses the hourly measures of road occupancy rates obtained from 862
29 sensors situated in the San Francisco Bay area freeways. These measurements were carried out
30 between January 2015 and December 2016.

31 (5) **SLEEPEEG** [6] contains 153 whole-night sleeping electroencephalography (EEG) recordings
32 from 82 healthy subjects. We follow the same data preprocessing approach as [25] to segment the
33 EEG signals without overlapping and get 371,055 univariate brainwaves. Each brainwave is sampled

Table 1: Dataset descriptions. *Samples* are organized in (Train/Validation/Test).

Tasks	Datasets	Channels	Length	Samples	Classes	Information	Frequency
Forecasting	ETTh1,ETTh2	7	{96,192,336,720}	8545/2881/2881	-	Electricity	1 Hour
	ETTh1,ETTh2	7	{96,192,336,720}	34465/11521/11521	-	Electricity	15 Mins
	Weather	21	{96,192,336,720}	36792/5271/10540	-	Weather	10 Mins
	Electricity	321	{96,192,336,720}	18317/2633/5261	-	Electricity	1 Hour
	Traffic	862	{96,192,336,720}	12185/1757/3509	-	Transportation	1 Hour
Classification	SleepEEG	1	200	371005/-/-	5	EEG	100 Hz
	Epilepsy	1	178	60/20/11420	2	EEG	174 Hz
	FD-B	1	5120	60/21/135599	3	Faulty Detection	64K Hz
	Gesture	3	315	320/120/120	8	Hand Movement	100 Hz
	EMG	1	1500	122/41/41	3	Muscle responses	4K Hz

34 at a frequency of 100 Hz and associated with one of five sleeping stages: Wake, Non-rapid eye
 35 movement (3 sub-states), and Rapid Eye Movement.

36 (6) **EPILEPSY** [1] monitors the brain activities of 500 subjects with a single-channel EEG sensor.
 37 Every subject is recorded for 23.6 seconds of brain activities. The dataset is sampled at 178 Hz and
 38 contains 11,500 samples in total. We follow the procedure described by [25]. The first four classes
 39 (eyes open, eyes closed, EEG measured in the healthy brain region, and EEG measured in the tumor
 40 region) of the original five categories of each sample are classified as positive, and the remaining
 41 classes (whether the subject has a seizure episode) are used as negative.

42 (7) **FD-B** [7] is generated by electromechanical drive systems. It monitors the condition of rolling
 43 bearings and detects their failures based on the monitoring conditions, which include speed, load
 44 torque, and radial force. Concretely, FD-B has 13,640 samples in total. Each recording is sampled at
 45 64k Hz with 3-class labels: undamaged, inner damaged, and outer damaged.

46 (8) **GESTURE** [9] are collected from 8 hand gestures based on the paths of hand movement recorded
 47 by an accelerometer. The eight gestures are hand swiping left, right, up, and down, hand waving in a
 48 counterclockwise or clockwise circle, hand waving in a square, and waving a right arrow, respectively.
 49 This dataset contains 440 examples of balanced classification labels that can be used, and each sample
 50 includes eight different kinds of gesture categories.

51 (9) **EMG** [14] is sampled with 4K Hz and consists of 163 single-channel EMG recordings from the
 52 anterior tibialis muscle of three healthy volunteers suffering from neuropathy and myopathy. Each
 53 patient is a classification category, so each sample is associated with one of three classes.

54 A.2 Baselines Implementation

55 We compare our proposed SimMTM against six state-of-the-art baselines. To make a fair and
 56 comprehensive comparison, we tried two baseline implementation approaches for forecasting and
 57 classification tasks: the unified encoder and reproduced with their official implementation encoder.
 58 Notably, the designs of LaST [17] and TF-C [25] are closely related to model structures. We directly
 59 report results from their papers or reproduce codes with official implementation.

60 (1) **Unified encoder.** We attempt to unify the encoder for these pre-training methods. Specifically,
 61 we adopt the vanilla Transformer [16] with channel independent [11] for forecasting to accomplish
 62 cross-domain transfer between datasets with different variate numbers. As for the classification, we
 63 use 1D-ResNet [5] as the encoder following [25]. Besides, we do a comprehensive hyperparameter

Table 2: Baselines implementation details.

Baselines	Task	Encoder	Performance Comparison	Report
Ti-MAE [8]	Forecasting	Channel-independent Transformer	better	Main text
		Official implementation		Section E
	Classification	1D-ResNet	better	Main text
		Official implementation		Section E
TST [24]	Forecasting	Channel-independent Transformer	better	Main text
		Official implementation		Section E
	Classification	1D-ResNet	better	Main text
		Official implementation		Section E
LaST [17]	Forecasting	Official implementation	/	Main text
	Classification	Official implementation	/	Main text
TF-C [25]	Forecasting	Official implementation	/	Main text
	Classification	Official implementation	/	Main text
CoST [20]	Forecasting	Channel-independent Transformer	better	Main text
		Official implementation		Section E
	Classification	1D-ResNet	better	Main text
		Official implementation		Section E
TS2Vec [23]	Forecasting	Channel-independent Transformer	better	Main text
		Official implementation		Section E
	Classification	1D-ResNet	better	Main text
		Official implementation		Section E

64 search for all baselines. For the Transformer encoder, we vary the number of Transformer layers
65 in $\{1, 2, 3, 4\}$, select the model dimension from $\{16, 32, 64, 128, 256\}$, and the attention head from
66 $\{4, 8, 16, 32\}$. For the 1D-ResNet, we search the number of 1D-ResNet layers from $\{1, 2, 3, 4\}$, the
67 kernel size from $\{3, 5, 8\}$ respectively. Additionally, for the masked modeling methods TST [24],
68 Ti-MAE [8], we also searched the masked ratio $r = \{0.125, 0.25, 0.5, 0.75\}$ for better performance.

69 (2) **Official implementation.** We also implement the baselines following the corresponding official
70 codes, including encoder, hyperparameters, etc. The comparisons are included in Section E of this
71 supplementary material. We directly report the results from their original papers for the same set. For
72 mismatched settings, the results are from our implementation.

73 Finally, for baselines Ti-MAE [8], TST [24], CoST [20], and TS2Vec [23], we report the results based
74 on the unified encoder in the main text. But for baselines LaST [17] and TF-C [25], we report the
75 results of the official code implementation or their original paper, which are limited by their model
76 structures. As a result, the performances of all baselines with unified encoder (that we reported in
77 the main text) generally surpass their official implementation and results reported in their own paper.
78 Table 2 shows more details. Full experimental results are in Section E.

79 A.3 Pre-training and Fine-tuning Configuration

80 We built two types of pre-training and fine-tuning scenarios, in-domain and cross-domain, based on
81 the benchmarks of forecasting and classification tasks to compare the effectiveness of our method
82 and other time series pre-training methods.

83 We pre-train a model on one subset for forecasting tasks and fine-tune it to the same dataset to
84 build seven in-domain transfer evaluation scenarios. In cross-domain evaluation, we pre-train a
85 model on one specific dataset and then use the other datasets for fine-tuning. Based on the above
86 settings, we constructed fifteen in-domain and cross-domain pre-training and fine-tuning experiments,
87 covering the same dataset with the same sampled frequency, different datasets with the same sampled
88 frequency, and different datasets with different sampled frequencies.

Table 3: Pre-training and fine-tuning scenarios for time series forecasting (Fore.) and classification (Class.) tasks, including the same and different datasets and in- and cross-domain settings.

Tasks	Evaluation	Scenarios	Characteristic
Fore.	In-domain	ETTh1 \rightarrow ETTh1	The same dataset with the same frequency
		ETTh2 \rightarrow ETTh2	
		ETTh1 \rightarrow ETTh2	
Fore.	Cross-domain	ETTh1 \rightarrow ETTh2	Different datasets with the same frequency.
		ETTh2 \rightarrow ETTh1	
		ETTh2 \rightarrow ETTh1	
Fore.	Cross-domain	{ETTh1, ETTh2, Weather} \rightarrow ETTh1	Different datasets with different frequencies.
		{ETTh1, ETTh2, Weather} \rightarrow ETTh2	
Class.	In-domain	Epilepsy \rightarrow Epilepsy	The same dataset with the same frequency.
	Cross-domain	SleepEEG \rightarrow {Epilepsy, FD-B, Gesture, EMG}	Different datasets with different frequencies.

89 We use the same dataset, Epilepsy, to construct the in-domain setting for classification tasks. For the
90 cross-domain setting, we pre-train a model for classification tasks on a univariate time series dataset
91 SleepEEG with the most complex temporal dynamics and the most samples. And then fine-tune
92 the model separately on Epilepsy, FD-B, Gesture, and EMG. Furthermore, we constructed four
93 cross-domain evaluation scenarios by pre-training from SleepEEG and fine-tuning to Epilepsy, FD-B,
94 Gesture, and EMG because of fewer commonalities and the enormous gap among these datasets.
95 Table 3 shows detailed pre-training and fine-tuning settings.

96 **A.4 Model and Training Configuration**

97 Following the previous convention, we choose the encoder part of Transformer [16] with channel
98 independent as the feature extractor for forecasting tasks. For the classification tasks, we adopt
99 1D-ResNet [5] as the encoder following [25]. In the pre-training stages, we pre-train the model
100 with different learning rates and batch sizes according to the pre-train datasets. Then we fine-tune
101 it to downstream forecasting and classification tasks supervised by L2 and Cross-Entropy losses,
102 respectively. The configuration details are in Table 4.

Table 4: Model and training configuration in Forecasting (Fore.) and Classification (Class.) tasks.

Tasks	Encoder		Pre-training			Fine-tuning			
	e_{layers}	d_{model}	learning rate	batch size	epochs	learning rate	loss function	batch size	epochs
Fore.	2	16	1e-3	32	50	1e-4	L2	{16,32}	10
Class.	3	128	1e-4	128	10	1e-4	Cross-Entropy	32	300

103 B Hyperparameter Sensitivity

104 We verify the hyperparameter sensitivity of the proposed time series pre-training method SimMTM
 105 on ETTh1 in Table 5, including masked ratio (r), the number of masked series (M), temperature (τ),
 106 masked function (Mask), encoder depth (e_{layers}), and the hidden dimension (d_{model}). Lower MSE
 107 and MAE represent better performance.

108 As shown in Table 5 (a) and 5 (b), we can observe the effect of the method is closely related to
 109 the trade-off of the masked ratio and the number of masked series. Hence, a reasonable balance
 110 between the two kinds of parameters is critical. For the temperature hyperparameter of softmax
 111 normalization (τ), we use an appropriately small τ that leads to higher differences and diversity of
 112 masked sequences. For the masked methods, we chose two masked methods for verification: masking
 113 following random distribution and masking following geometric distribution [24]. The results show
 114 that the method based on geometric masking is better than random masking modeling. Besides,
 115 we can find that 2 encoder layers are enough for reconstruction tasks. Note our method SimMTM
 116 consistently performs better than training from scratch under various hyperparameter changes.

Table 5: Hyperparameter sensitivity experiments on ETTh1 for the in-domain setting. The entries marked in bold are the same which specify the default settings. This table format follows [4].

(a) Masked ratio			(b) Masked numbers			(c) Temperature		
Ratio	MSE	MAE	Numbers	MSE	MAE	Value	MSE	MAE
12.5%	0.429	0.440	1	0.429	0.437	0.02	0.409	0.428
25%	0.427	0.434	2	0.416	0.429	0.2	0.409	0.429
50%	0.409	0.428	3	0.409	0.428	2	0.416	0.428
75%	0.422	0.434	4	0.419	0.431			
(d) Masked function			(e) Encoder depth			(f) Hidden layer dimension		
Type	MSE	MAE	Layers	MSE	MAE	Dim	MSE	MAE
Random	0.409	0.431	1	0.420	0.426	16	0.409	0.428
Geometric	0.409	0.428	2	0.409	0.428	32	0.420	0.432
			3	0.421	0.430	64	0.422	0.434
			4	0.426	0.436	128	0.428	0.444

117 C Ablations on Aggregation Setting

118 SimMTM proposes to recover masked time points by the weighted aggregation of multiple neighbors
 119 outside the manifold. We explored two types of aggregation settings.

120 (1) **Positive Samples Aggregation (PSA)**: only aggregate multiple positive neighbors (the masked
 121 series of the same sample) to reconstruct masked time points.

122 (2) **Positive and Negative Samples Aggregation (PNSA)**: aggregate both positive and negative
 123 neighbors (the masked series of all samples) to reconstruct masked time points.

124 As shown in Table 6, although PSA made good progress compared to training from scratch (Random
 125 Init.), PNSA is consistently better than SimMTM PSA in all ablation settings. In masked time-series
 126 modeling, masking can be viewed as adding noise to the original data, and masked modeling is
 127 to project masked data from the neighborhood back to the original manifold. We use positive and
 128 negative masked time series as the reconstruction candidates to drive the model to select the positive
 129 samples adaptively, which can make the model learn the structure of the manifold better. Therefore,
 130 as stated in the Method Section of the main text, we choose positive and negative sample aggregation
 131 (PNSA) as the standard aggregation setting of SimMTM.

Table 6: Ablations on aggregation setting in forecasting (MSE) and classification (Acc) tasks for in- and cross-domain settings. A smaller MSE or a higher Accuracy indicates a better result (\uparrow).

Tasks	Evaluation	Scenarios	Aggregation	Metric
Forecasting	In-domain	ETTh1 \rightarrow ETTh1	Random init.	0.431
			SimMTM (PSA)	0.420 \uparrow
	Cross-domain	ETTh2 \rightarrow ETTh1	Random init.	0.431
			SimMTM (PNSA)	0.415 \uparrow
Classification	In-domain	Epilepsy \rightarrow Epilepsy	Random init.	89.83
			SimMTM (PSA)	92.56 \uparrow
	Cross-domain	SleepEEG \rightarrow EMG	Random init.	77.80
			SimMTM (PNSA)	97.56 \uparrow

132 D Comparison of Masked Modeling

133 To investigate the reconstruction process of different masked modeling methods, we plot both
 134 original and reconstructed time series from TST and SimMTM in Figure 1, where TST [24] follows
 135 the canonical masked modeling paradigm and learns to predict removed time points based on the
 136 remaining time points. In Figure 1, we can find that direct reconstruction is too difficult in time
 137 series, even for the 12.5% masking ratio. As for the 75% masking ratio, TST degenerates more
 138 seriously. Because of this poor reconstruction effect, direct reconstruction is difficult to provide
 139 reliable guidance to model pre-training. In contrast, our proposed SimMTM can precisely reconstruct
 140 the original time series, benefiting the representation learning. These results also support our design
 141 in neighborhood reconstruction.

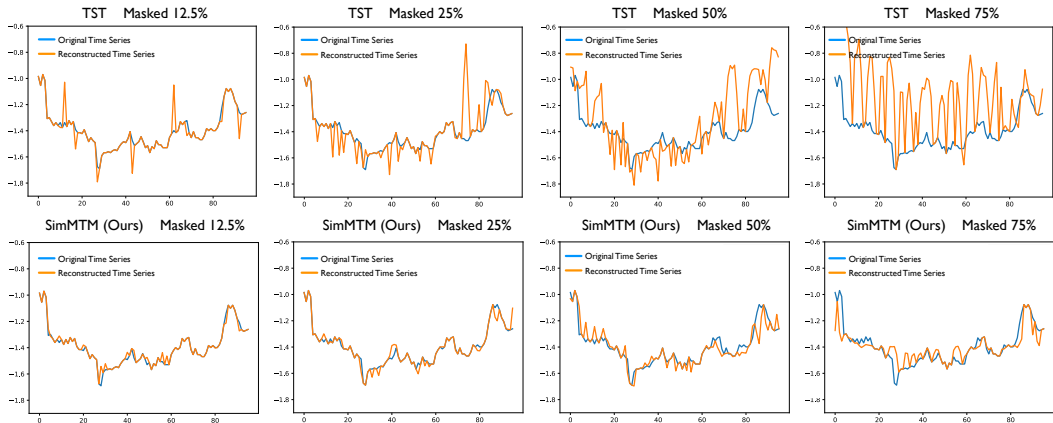


Figure 1: Comparison of the canonical masked modeling paradigm TST and neighborhood aggregation masked modeling SimMTM in reconstructing time series. All the cases are shown from ETTh1.

142 **E Full Results**

143 Due to the limited length of the text, we summarize all the experiments in the main text into two parts:
 144 the main experiment and the analytical experiment. We categorize and index them in Tabel 7, 8.

Table 7: The main results of pre-training and fine-tuning scenarios for time series forecasting and classification tasks, including the same and different encoder for in- and cross-domain settings.

Tasks	Evaluation	Encoder	Labels Name
Forecasting	In-domain	The model utilized in the original papers	Table 9
		Transformer with channel independent	Table 10
	Cross-domain	The model utilized in the original papers	Table 11
		Transformer with channel independent	Table 12
Classification	In-domain	The model utilized in the original papers	Table 17
		1D-ResNet	Table 18
	Cross-domain	The model utilized in the original papers	Table 17
		1D-ResNet	Table 18

Table 8: The model analysis results of pre-training and fine-tuning scenarios for time series forecasting and classification tasks with the unified encoder for in- and cross-domain settings.

Tasks	Evaluation	Analysis	Labels Name
Forecasting	In-domain	Ablation study	Table 13
		Model generality	Table 15
	Cross-domain	Ablation study	Table 14
		Limited data	Table 16
Classification	In-domain	Ablation study	Table 19
	Cross-domain	Ablation study	Table 19

145 **F Limitations**

146 SimMTM is inspired by the manifold perspective of masked modeling. Although we have provided
 147 relatively comprehensive results to verify the model’s effectiveness, the model performance still
 148 needs theoretical guarantees. In fact, the most high-impact works in the self-supervised pre-training
 149 community are without theoretical analysis, such as BERT [2], GPT-3 [3], MAE [4] and SimMIM
 150 [22]. Thus, we would like to leave this problem as a future work.

151 The masking ratio of masked modeling methods is an essential hyper-parameter. Although we have
 152 provided a chosen principle to masking ratio r and the number of masked time series M as $M \propto r$
 153 in the main text, we still need to tune these two hyperparameters for different datasets to achieve the best
 154 performance. Notably, previous methods also chose the masking ratio solely based on the empirical
 155 results [2, 4]. Thus, despite there exist limitations of SimMTM in choosing hyperparameters, the
 156 principle of $M \propto r$ can somewhat ease this problem. And the chosen strategy of the masking ratio
 157 can also be a potential topic in masked modeling [19].

158 **G Social Impacts**

159 This paper presents SimMTM as a new masked modeling method for time series. SimMTM achieves
 160 state-of-the-art in two mainstream time series analysis tasks, which can be a good supplement for the
 161 self-supervised pre-training community. We will also publish the codebase of time-series pre-training
 162 to facilitate future research.

163 This paper only focuses on the algorithm design. Using all the codes and datasets strictly follows the
 164 corresponding licenses (Appendix A.1). There is no potential ethical risk or negative social impact.

Table 9: Complete results of long-term forecasting tasks for the in-domain setting of forecasting the future $O \in \{96, 192, 336, 720\}$ time points based on the past 336 time points. **All the results of baselines are based on the encoder utilized in their original papers.** The standard deviations of SimMTM are within 0.005 for MSE and within 0.004 for MAE.

Models	SimMTM	Random init.	Ti-MAE [8]	TST [24]	LaST [17]	TF-C [25]	CoST [20]	TS2Vec [23]	
Metric	MSE MAE	MSE MAE	MSE MAE	MSE MAE	MSE MAE	MSE MAE	MSE MAE	MSE MAE	
ETTh1	96	0.379 0.407	0.380 0.412	0.708 0.570	0.503 0.527	0.399 0.412	0.463 0.406	0.514 0.512	0.709 0.650
	192	0.412 0.424	0.416 0.434	0.725 0.587	0.601 0.552	0.484 0.468	0.531 0.540	0.655 0.590	0.927 0.757
	336	0.421 0.431	0.448 0.458	0.713 0.589	0.625 0.541	0.580 0.533	0.535 0.545	0.790 0.666	0.986 0.811
	720	0.424 0.449	0.481 0.487	0.736 0.618	0.768 0.628	0.432 0.432	0.577 0.562	0.880 0.739	0.967 0.790
	Avg	0.409 0.428	0.431 0.448	0.721 0.591	0.624 0.562	0.474 0.461	0.527 0.513	0.710 0.627	0.897 0.752
ETTh2	96	0.293 0.347	0.325 0.374	0.443 0.465	0.335 0.392	0.331 0.390	0.463 0.521	0.465 0.482	0.506 0.477
	192	0.355 0.386	0.400 0.424	0.533 0.516	0.444 0.441	0.451 0.452	0.525 0.561	0.671 0.599	0.567 0.547
	336	0.370 0.401	0.405 0.433	0.445 0.472	0.455 0.494	0.460 0.478	0.850 0.883	0.848 0.776	0.694 0.628
	720	0.395 0.427	0.451 0.475	0.507 0.498	0.481 0.504	0.552 0.509	0.930 0.932	0.871 0.811	0.728 0.838
	Avg	0.353 0.390	0.395 0.427	0.482 0.488	0.429 0.458	0.449 0.457	0.692 0.724	0.714 0.667	0.624 0.623
ETTml	96	0.288 0.348	0.295 0.346	0.647 0.497	0.454 0.456	0.316 0.355	0.419 0.401	0.376 0.420	0.563 0.551
	192	0.327 0.373	0.333 0.374	0.597 0.508	0.471 0.490	0.349 0.366	0.471 0.438	0.420 0.451	0.599 0.558
	336	0.363 0.395	0.370 0.398	0.699 0.525	0.457 0.451	0.429 0.407	0.540 0.509	0.482 0.494	0.685 0.594
	720	0.412 0.424	0.427 0.431	0.786 0.596	0.594 0.488	0.496 0.464	0.552 0.548	0.628 0.578	0.831 0.698
	Avg	0.348 0.385	0.356 0.387	0.682 0.532	0.494 0.471	0.398 0.398	0.496 0.474	0.477 0.486	0.670 0.600
ETTm2	96	0.172 0.261	0.175 0.268	0.304 0.357	0.363 0.301	0.163 0.255	0.401 0.477	0.276 0.384	0.448 0.482
	192	0.223 0.300	0.240 0.312	0.334 0.387	0.342 0.364	0.239 0.303	0.422 0.490	0.500 0.532	0.545 0.536
	336	0.282 0.331	0.298 0.351	0.420 0.441	0.414 0.361	0.259 0.366	0.513 0.508	0.680 0.695	0.681 0.744
	720	0.374 0.388	0.403 0.413	0.508 0.481	0.580 0.456	0.397 0.382	0.523 0.772	0.925 0.914	0.691 0.837
	Avg	0.263 0.320	0.279 0.336	0.392 0.417	0.425 0.371	0.265 0.327	0.465 0.562	0.595 0.631	0.591 0.650
Weather	96	0.158 0.211	0.166 0.216	0.216 0.280	0.292 0.370	0.153 0.211	0.215 0.296	0.327 0.359	0.433 0.462
	192	0.199 0.249	0.208 0.254	0.303 0.335	0.410 0.473	0.207 0.250	0.267 0.345	0.390 0.422	0.508 0.518
	336	0.246 0.286	0.257 0.290	0.351 0.358	0.434 0.427	0.249 0.264	0.299 0.360	0.477 0.446	0.545 0.549
	720	0.317 0.337	0.326 0.338	0.425 0.399	0.539 0.523	0.319 0.320	0.361 0.395	0.551 0.586	0.576 0.572
	Avg	0.230 0.271	0.239 0.275	0.324 0.343	0.419 0.448	0.232 0.261	0.286 0.349	0.436 0.453	0.516 0.525
Electricity	96	0.133 0.223	0.190 0.279	0.399 0.412	0.292 0.370	0.166 0.254	0.366 0.436	0.230 0.353	0.322 0.401
	192	0.147 0.237	0.195 0.285	0.400 0.460	0.270 0.373	0.178 0.278	0.366 0.433	0.253 0.371	0.343 0.416
	336	0.166 0.265	0.211 0.301	0.564 0.573	0.334 0.323	0.186 0.275	0.358 0.428	0.197 0.287	0.362 0.435
	720	0.203 0.297	0.253 0.333	0.880 0.770	0.344 0.346	0.213 0.288	0.363 0.431	0.230 0.328	0.388 0.456
	Avg	0.162 0.256	0.212 0.300	0.561 0.554	0.310 0.353	0.186 0.274	0.363 0.432	0.228 0.335	0.354 0.427
Traffic	96	0.368 0.262	0.471 0.309	0.431 0.482	0.559 0.454	0.706 0.385	0.613 0.340	0.751 0.431	0.321 0.367
	192	0.373 0.251	0.475 0.308	0.491 0.346	0.583 0.493	0.709 0.388	0.619 0.516	0.751 0.424	0.476 0.367
	336	0.395 0.254	0.490 0.315	0.502 0.384	0.637 0.469	0.714 0.394	0.785 0.497	0.761 0.425	0.499 0.376
	720	0.432 0.290	0.524 0.332	0.533 0.543	0.663 0.594	0.723 0.421	0.850 0.472	0.780 0.433	0.563 0.390
	Avg	0.392 0.264	0.490 0.316	0.489 0.399	0.611 0.503	0.713 0.397	0.717 0.456	0.761 0.428	0.501 0.375

Table 10: Complete results of long-term forecasting tasks for the in-domain setting of forecasting the future $O \in \{96, 192, 336, 720\}$ time points based on the past 336 time points. **All the results of baseline are based on the unified channel-independent Transformer encoder.** The standard deviations of SimMTM are within 0.005 for MSE and within 0.004 for MAE.

Models	SimMTM	Random init.	Ti-MAE [8]		TST [24]		LaST [17]		TF-C [25]		CoST [20]		TS2Vec [23]				
Metric	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE			
ETTh1	96	0.379	0.407	0.380	0.412	0.356	0.420	0.401	0.425	-	-	-	-	0.422	0.436	0.392	0.420
	192	0.412	0.424	0.416	0.434	0.421	0.434	0.427	0.432	-	-	-	-	0.520	0.487	0.445	0.452
	336	0.421	0.431	0.448	0.458	0.447	0.446	0.519	0.487	-	-	-	-	0.472	0.462	0.453	0.455
	720	0.424	0.449	0.481	0.487	0.469	0.482	0.515	0.504	-	-	-	-	0.525	0.501	0.495	0.496
	Avg	0.409	0.428	0.431	0.448	0.423	0.446	0.466	0.462	-	-	-	-	0.485	0.472	0.446	0.456
ETTh2	96	0.293	0.347	0.325	0.374	0.339	0.378	0.322	0.358	-	-	-	-	0.321	0.374	0.365	0.509
	192	0.355	0.386	0.400	0.424	0.380	0.402	0.448	0.435	-	-	-	-	0.380	0.403	0.396	0.422
	336	0.370	0.401	0.405	0.433	0.388	0.323	0.420	0.440	-	-	-	-	0.430	0.451	0.399	0.436
	720	0.395	0.427	0.451	0.475	0.414	0.442	0.424	0.452	-	-	-	-	0.466	0.480	0.508	0.503
	Avg	0.353	0.390	0.395	0.427	0.380	0.386	0.404	0.421	-	-	-	-	0.399	0.427	0.417	0.468
ETTm1	96	0.288	0.348	0.295	0.346	0.305	0.351	0.310	0.348	-	-	-	-	0.291	0.343	0.681	0.689
	192	0.327	0.373	0.333	0.374	0.343	0.374	0.362	0.380	-	-	-	-	0.330	0.370	0.689	0.551
	336	0.363	0.395	0.370	0.398	0.387	0.407	0.389	0.402	-	-	-	-	0.382	0.401	0.704	0.559
	720	0.412	0.424	0.427	0.431	0.428	0.432	0.433	0.427	-	-	-	-	0.422	0.425	0.721	0.571
	Avg	0.348	0.385	0.356	0.387	0.366	0.391	0.373	0.389	-	-	-	-	0.356	0.385	0.699	0.557
ETTm2	96	0.172	0.261	0.175	0.268	0.174	0.258	0.215	0.296	-	-	-	-	0.242	0.333	0.224	0.303
	192	0.223	0.300	0.240	0.312	0.257	0.303	0.259	0.323	-	-	-	-	0.283	0.345	0.273	0.331
	336	0.282	0.331	0.298	0.351	0.277	0.333	0.319	0.364	-	-	-	-	0.303	0.349	0.399	0.402
	720	0.374	0.388	0.403	0.413	0.360	0.404	0.395	0.405	-	-	-	-	0.431	0.431	0.406	0.408
	Avg	0.263	0.320	0.279	0.336	0.267	0.325	0.297	0.347	-	-	-	-	0.314	0.365	0.326	0.361
Weather	96	0.158	0.211	0.166	0.216	0.153	0.196	0.162	0.214	-	-	-	-	0.216	0.280	0.154	0.205
	192	0.199	0.249	0.208	0.254	0.214	0.253	0.203	0.252	-	-	-	-	0.303	0.335	0.200	0.243
	336	0.246	0.286	0.257	0.290	0.243	0.272	0.260	0.297	-	-	-	-	0.351	0.358	0.252	0.286
	720	0.317	0.337	0.326	0.338	0.324	0.349	0.330	0.342	-	-	-	-	0.425	0.343	0.324	0.335
	Avg	0.230	0.271	0.239	0.275	0.234	0.265	0.239	0.276	-	-	-	-	0.324	0.329	0.233	0.267
Electricity	96	0.133	0.223	0.190	0.279	0.163	0.255	0.186	0.268	-	-	-	-	0.197	0.277	0.195	0.275
	192	0.147	0.237	0.195	0.285	0.194	0.288	0.193	0.276	-	-	-	-	0.197	0.279	0.195	0.277
	336	0.166	0.265	0.211	0.301	0.201	0.298	0.206	0.289	-	-	-	-	0.211	0.295	0.210	0.294
	720	0.203	0.297	0.253	0.333	0.263	0.343	0.250	0.324	-	-	-	-	0.255	0.330	0.252	0.327
	Avg	0.162	0.256	0.212	0.300	0.205	0.296	0.209	0.289	-	-	-	-	0.215	0.295	0.213	0.293
Traffic	96	0.368	0.262	0.471	0.309	0.448	0.298	0.595	0.360	-	-	-	-	0.378	0.365	0.480	0.357
	192	0.373	0.251	0.475	0.308	0.445	0.301	0.576	0.353	-	-	-	-	0.371	0.352	0.439	0.336
	336	0.395	0.254	0.490	0.315	0.492	0.320	0.569	0.362	-	-	-	-	0.467	0.354	0.460	0.344
	720	0.432	0.290	0.524	0.332	0.514	0.321	0.603	0.372	-	-	-	-	0.525	0.378	0.499	0.364
	Avg	0.392	0.264	0.490	0.316	0.475	0.310	0.586	0.362	-	-	-	-	0.435	0.362	0.470	0.350

Table 11: Complete results of long-term forecasting tasks for the cross-domain setting of forecasting the future $O \in \{96, 192, 336, 720\}$ time points based on the past 336 time points. **All the results of baselines are based on the encoder utilized in their original papers.** The standard deviations of SimMTM are within 0.005 for MSE and within 0.004 for MAE.

Models	SimMTM		Random init.		Ti-MAE [8]		TST [24]		LaST [17]		TF-C [25]		CoST [20]		TS2Vec [23]		
Metric	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	
ETTh2 ↓ ETTh1	96	0.372	0.401	0.380	0.412	0.703	0.562	0.653	0.468	0.362	0.420	0.596	0.569	0.378	0.421	0.849	0.694
	192	0.414	0.425	0.416	0.434	0.715	0.567	0.658	0.502	0.426	0.478	0.614	0.621	0.424	0.451	0.909	0.738
	336	0.429	0.436	0.448	0.458	0.733	0.579	0.631	0.561	0.522	0.509	0.694	0.664	0.651	0.582	1.082	0.775
	720	0.446	0.458	0.481	0.487	0.762	0.622	0.638	0.608	0.460	0.478	0.635	0.683	0.883	0.701	0.934	0.769
	Avg	0.415	0.430	0.431	0.448	0.728	0.583	0.645	0.535	0.443	0.471	0.635	0.634	0.584	0.539	0.944	0.744
ETTh1 ↓ ETTh1	96	0.367	0.398	0.380	0.412	0.715	0.581	0.627	0.477	0.360	0.374	0.666	0.647	0.423	0.450	0.991	0.765
	192	0.396	0.421	0.416	0.434	0.729	0.587	0.628	0.500	0.381	0.371	0.672	0.653	0.641	0.578	0.829	0.699
	336	0.471	0.437	0.448	0.458	0.712	0.583	0.683	0.554	0.472	0.531	0.626	0.711	0.863	0.694	0.971	0.787
	720	0.454	0.463	0.481	0.487	0.747	0.627	0.642	0.600	0.490	0.488	0.835	0.797	1.071	0.805	1.037	0.820
	Avg	0.422	0.430	0.431	0.448	0.726	0.595	0.645	0.533	0.426	0.441	0.700	0.702	0.750	0.632	0.957	0.768
ETTh2 ↓ ETTh1	96	0.388	0.421	0.380	0.412	0.699	0.566	0.559	0.489	0.428	0.454	0.968	0.738	0.377	0.419	0.783	0.669
	192	0.419	0.423	0.416	0.434	0.722	0.573	0.600	0.579	0.427	0.497	1.080	0.801	0.422	0.450	0.828	0.691
	336	0.435	0.444	0.448	0.458	0.714	0.569	0.677	0.572	0.528	0.540	1.091	0.824	0.648	0.580	0.990	0.762
	720	0.468	0.474	0.481	0.487	0.760	0.611	0.694	0.664	0.527	0.537	1.226	0.893	0.880	0.699	0.985	0.783
	Avg	0.428	0.441	0.431	0.448	0.724	0.580	0.632	0.576	0.503	0.507	1.091	0.814	0.582	0.537	0.896	0.726
Weather ↓ ETTh1	96	0.477	0.444	0.380	0.412	-	-	-	-	-	-	-	-	-	-	-	-
	192	0.454	0.522	0.416	0.434	-	-	-	-	-	-	-	-	-	-	-	-
	336	0.424	0.434	0.448	0.458	-	-	-	-	-	-	-	-	-	-	-	-
	720	0.468	0.469	0.481	0.487	-	-	-	-	-	-	-	-	-	-	-	-
	Avg	0.456	0.467	0.431	0.448	-	-	-	-	-	-	-	-	-	-	-	-
ETTh1 ↓ ETTh1	96	0.290	0.348	0.295	0.346	0.667	0.521	0.425	0.381	0.295	0.387	0.672	0.600	0.248	0.332	0.605	0.561
	192	0.327	0.372	0.333	0.374	0.561	0.479	0.495	0.478	0.335	0.379	0.721	0.639	0.336	0.391	0.615	0.561
	336	0.357	0.392	0.370	0.398	0.690	0.533	0.456	0.441	0.379	0.363	0.755	0.664	0.381	0.421	0.763	0.677
	720	0.409	0.423	0.427	0.431	0.744	0.583	0.554	0.477	0.403	0.431	0.837	0.705	0.469	0.482	0.805	0.664
	Avg	0.346	0.384	0.356	0.387	0.666	0.529	0.482	0.444	0.353	0.390	0.746	0.652	0.359	0.407	0.697	0.616
ETTh2 ↓ ETTh1	96	0.322	0.347	0.295	0.346	0.658	0.505	0.449	0.343	0.314	0.396	0.677	0.603	0.253	0.342	0.466	0.480
	192	0.332	0.372	0.333	0.374	0.594	0.511	0.477	0.407	0.587	0.545	0.718	0.638	0.367	0.392	0.557	0.532
	336	0.394	0.391	0.370	0.398	0.732	0.532	0.407	0.519	0.631	0.584	0.755	0.663	0.388	0.431	0.646	0.576
	720	0.411	0.424	0.427	0.431	0.768	0.592	0.557	0.523	0.368	0.429	0.848	0.712	0.498	0.488	0.752	0.638
	Avg	0.365	0.384	0.356	0.387	0.688	0.535	0.472	0.448	0.475	0.489	0.750	0.654	0.377	0.413	0.606	0.556
ETTh2 ↓ ETTh1	96	0.297	0.348	0.295	0.346	0.647	0.497	0.471	0.422	0.304	0.388	0.610	0.577	0.239	0.331	0.586	0.515
	192	0.332	0.370	0.333	0.374	0.597	0.508	0.495	0.442	0.429	0.494	0.725	0.657	0.339	0.371	0.624	0.562
	336	0.364	0.393	0.370	0.398	0.700	0.525	0.455	0.424	0.499	0.523	0.768	0.684	0.371	0.421	1.035	0.806
	720	0.410	0.421	0.427	0.431	0.786	0.596	0.498	0.532	0.422	0.450	0.927	0.759	0.467	0.481	0.780	0.669
	Avg	0.351	0.383	0.356	0.387	0.682	0.531	0.480	0.455	0.414	0.464	0.758	0.669	0.354	0.401	0.756	0.638
Weather ↓ ETTh1	96	0.304	0.354	0.295	0.346	-	-	-	-	-	-	-	-	-	-	-	-
	192	0.338	0.375	0.333	0.374	-	-	-	-	-	-	-	-	-	-	-	-
	336	0.371	0.397	0.370	0.398	-	-	-	-	-	-	-	-	-	-	-	-
	720	0.417	0.426	0.427	0.431	-	-	-	-	-	-	-	-	-	-	-	-
	Avg	0.358	0.388	0.356	0.387	-	-	-	-	-	-	-	-	-	-	-	-

Table 12: Complete results of long-term forecasting tasks for the in-domain setting. **All the results of baseline are based on the unified channel-independent Transformer encoder.** The past sequence length is set as 336. The unified channel-independent transformer model can perform the transfer experiment between datasets with different variables. The standard deviations of SimMTM are within 0.005 for MSE and within 0.004 for MAE.

Models		SimMTM		Random init.		Ti-MAE [8]		TST [24]		LaST [17]		TF-C [25]		CoST [20]		TS2Vec [23]	
Metric		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ETTh2 ↓ ETTh1	96	0.372	0.401	0.380	0.412	0.399	0.424	0.401	0.425	-	-	-	-	0.376	0.362	0.436	0.430
	192	0.414	0.425	0.416	0.434	0.454	0.440	0.531	0.484	-	-	-	-	0.376	0.362	0.455	0.440
	336	0.429	0.436	0.448	0.458	0.497	0.469	0.474	0.459	-	-	-	-	0.444	0.444	0.689	0.584
	720	0.446	0.458	0.481	0.487	0.515	0.492	0.471	0.469	-	-	-	-	0.517	0.510	0.489	0.490
	Avg	0.415	0.430	0.431	0.448	0.466	0.456	0.469	0.459	-	-	-	-	0.428	0.433	0.517	0.486
ETTh1 ↓ ETTh1	96	0.367	0.398	0.380	0.412	0.400	0.418	0.443	0.440	-	-	-	-	0.465	0.456	0.413	0.443
	192	0.396	0.421	0.416	0.434	0.434	0.445	0.471	0.455	-	-	-	-	0.722	0.588	0.459	0.465
	336	0.471	0.437	0.448	0.458	0.510	0.467	0.462	0.455	-	-	-	-	0.712	0.586	0.614	0.554
	720	0.454	0.463	0.481	0.487	0.636	0.544	0.525	0.503	-	-	-	-	0.581	0.533	0.450	0.464
	Avg	0.422	0.430	0.431	0.448	0.495	0.469	0.475	0.463	-	-	-	-	0.620	0.541	0.484	0.482
ETTh2 ↓ ETTh1	96	0.388	0.421	0.380	0.412	0.433	0.431	0.389	0.413	-	-	-	-	0.403	0.426	0.483	0.480
	192	0.419	0.423	0.416	0.434	0.474	0.458	0.463	0.452	-	-	-	-	0.457	0.468	0.579	0.537
	336	0.435	0.444	0.448	0.458	0.515	0.448	0.492	0.465	-	-	-	-	0.794	0.682	0.673	0.563
	720	0.468	0.474	0.481	0.487	0.496	0.488	0.468	0.468	-	-	-	-	0.739	0.617	0.729	0.620
	Avg	0.428	0.441	0.431	0.448	0.464	0.456	0.453	0.450	-	-	-	-	0.598	0.548	0.616	0.550
Weather ↓ ETTh1	96	0.477	0.444	0.380	0.412	0.397	0.440	0.428	0.429	-	-	-	-	0.421	0.410	0.393	0.410
	192	0.454	0.522	0.416	0.434	0.458	0.466	0.461	0.451	-	-	-	-	0.539	0.503	0.440	0.437
	336	0.424	0.434	0.448	0.458	0.479	0.458	0.463	0.456	-	-	-	-	0.568	0.514	0.450	0.451
	720	0.468	0.469	0.481	0.487	0.515	0.492	0.507	0.489	-	-	-	-	0.544	0.522	0.567	0.541
	Avg	0.456	0.467	0.431	0.448	0.462	0.464	0.465	0.456	-	-	-	-	0.518	0.487	0.463	0.460
ETTh1 ↓ ETTh1	96	0.290	0.348	0.295	0.346	0.311	0.355	0.315	0.354	-	-	-	-	0.308	0.355	0.681	0.545
	192	0.327	0.372	0.333	0.374	0.337	0.372	0.365	0.391	-	-	-	-	0.357	0.390	0.689	0.551
	336	0.357	0.392	0.370	0.398	0.372	0.398	0.384	0.400	-	-	-	-	0.396	0.402	0.705	0.560
	720	0.409	0.423	0.427	0.431	0.422	0.433	0.428	0.426	-	-	-	-	0.419	0.423	0.722	0.571
	Avg	0.346	0.384	0.356	0.387	0.360	0.390	0.373	0.393	-	-	-	-	0.370	0.393	0.699	0.557
ETTh2 ↓ ETTh1	96	0.322	0.347	0.295	0.346	0.323	0.362	0.338	0.383	-	-	-	-	0.322	0.351	0.679	0.546
	192	0.332	0.372	0.333	0.374	0.370	0.395	0.394	0.408	-	-	-	-	0.331	0.373	0.673	0.551
	336	0.394	0.391	0.370	0.398	0.397	0.413	0.401	0.412	-	-	-	-	0.382	0.397	0.703	0.557
	720	0.411	0.424	0.427	0.431	0.442	0.439	0.434	0.432	-	-	-	-	0.417	0.428	0.722	0.573
	Avg	0.365	0.384	0.356	0.387	0.383	0.402	0.391	0.409	-	-	-	-	0.363	0.387	0.694	0.557
ETTh2 ↓ ETTh1	96	0.297	0.348	0.295	0.346	0.333	0.378	0.327	0.364	-	-	-	-	0.320	0.364	0.422	0.434
	192	0.332	0.370	0.333	0.374	0.381	0.398	0.362	0.389	-	-	-	-	0.367	0.386	0.387	0.371
	336	0.364	0.393	0.370	0.398	0.394	0.413	0.401	0.418	-	-	-	-	0.374	0.394	0.402	0.444
	720	0.410	0.421	0.427	0.431	0.455	0.453	0.437	0.437	-	-	-	-	0.479	0.503	0.481	0.432
	Avg	0.351	0.383	0.356	0.387	0.390	0.410	0.382	0.402	-	-	-	-	0.385	0.412	0.423	0.420
Weather ↓ ETTh1	96	0.294	0.354	0.295	0.346	0.338	0.380	0.324	0.366	-	-	-	-	0.324	0.360	0.329	0.359
	192	0.318	0.355	0.333	0.374	0.473	0.457	0.349	0.377	-	-	-	-	0.359	0.387	0.392	0.392
	336	0.361	0.397	0.370	0.398	0.402	0.415	0.378	0.398	-	-	-	-	0.395	0.399	0.372	0.400
	720	0.427	0.426	0.427	0.431	0.432	0.438	0.422	0.427	-	-	-	-	0.450	0.467	0.434	0.429
	Avg	0.350	0.383	0.356	0.387	0.411	0.423	0.368	0.392	-	-	-	-	0.382	0.403	0.382	0.395

Table 13: Full ablation studies for the in-domain setting of forecasting. The standard deviations of SimMTM are within 0.005 for MSE and within 0.004 for MAE.

Input-336		Supervised		W/o $\mathcal{L}_{reconstruction}$		W/o $\mathcal{L}_{constraint}$		SimMTM	
Metric		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ETTh1	96	0.380	0.412	0.377	0.408	0.381	0.409	0.379	0.407
	192	0.416	0.434	0.419	0.443	0.409	0.443	0.412	0.424
	336	0.448	0.458	0.423	0.434	0.432	0.444	0.421	0.431
	720	0.481	0.487	0.437	0.454	0.447	0.454	0.424	0.449
	Avg	0.431	0.448	0.414	0.435	0.417	0.438	0.409	0.428
ETTh2	96	0.325	0.374	0.288	0.344	0.312	0.365	0.293	0.347
	192	0.400	0.424	0.356	0.391	0.389	0.418	0.355	0.386
	336	0.405	0.433	0.368	0.406	0.396	0.432	0.370	0.401
	720	0.451	0.475	0.409	0.432	0.448	0.479	0.395	0.427
	Avg	0.395	0.427	0.355	0.393	0.386	0.424	0.353	0.390
ETTh1	96	0.295	0.346	0.291	0.343	0.282	0.337	0.288	0.348
	192	0.333	0.374	0.330	0.390	0.324	0.388	0.327	0.373
	336	0.370	0.398	0.369	0.399	0.366	0.397	0.363	0.395
	720	0.427	0.431	0.417	0.429	0.424	0.435	0.412	0.424
	Avg	0.356	0.387	0.352	0.390	0.349	0.389	0.348	0.385
ETTh2	96	0.175	0.268	0.174	0.265	0.170	0.261	0.172	0.261
	192	0.240	0.312	0.232	0.303	0.244	0.320	0.223	0.300
	336	0.298	0.351	0.313	0.365	0.279	0.334	0.282	0.331
	720	0.403	0.413	0.376	0.451	0.376	0.378	0.374	0.388
	Avg	0.279	0.336	0.274	0.346	0.267	0.323	0.263	0.320
Weather	96	0.166	0.216	0.164	0.209	0.160	0.212	0.158	0.211
	192	0.208	0.254	0.203	0.258	0.203	0.251	0.199	0.249
	336	0.257	0.290	0.244	0.289	0.253	0.290	0.246	0.286
	720	0.326	0.338	0.322	0.343	0.325	0.340	0.317	0.337
	Avg	0.239	0.275	0.233	0.275	0.235	0.273	0.230	0.271
Electricity	96	0.190	0.279	0.177	0.270	0.134	0.220	0.133	0.223
	192	0.195	0.285	0.184	0.279	0.163	0.274	0.147	0.237
	336	0.211	0.301	0.202	0.300	0.223	0.311	0.166	0.265
	720	0.253	0.333	0.250	0.337	0.241	0.321	0.203	0.297
	Avg	0.212	0.300	0.203	0.397	0.190	0.282	0.162	0.256
Traffic	96	0.471	0.309	0.366	0.257	0.457	0.301	0.368	0.262
	192	0.475	0.308	0.373	0.266	0.468	0.325	0.373	0.251
	336	0.490	0.315	0.401	0.249	0.487	0.302	0.395	0.254
	720	0.524	0.332	0.472	0.312	0.485	0.315	0.432	0.290
	Avg	0.490	0.316	0.403	0.271	0.474	0.311	0.392	0.264

Table 14: Full ablation studies on transfer to ETTh1 and ETTm1 for the cross-domain setting of forecasting. The standard deviations of SimMTM are within 0.005 for MSE and within 0.004 for MAE.

Input-336 Metric		Supervised		W/o $\mathcal{L}_{\text{reconstruction}}$		W/o $\mathcal{L}_{\text{constraint}}$		SimMTM	
		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ETTh2 ↓ ETTh1	96	0.380	0.412	0.377	0.400	0.402	0.411	0.372	0.401
	192	0.416	0.434	0.417	0.424	0.417	0.420	0.414	0.425
	336	0.448	0.458	0.437	0.439	0.437	0.435	0.429	0.436
	720	0.481	0.487	0.448	0.463	0.456	0.467	0.446	0.458
	Avg	0.431	0.448	0.420	0.432	0.423	0.430	0.415	0.430
ETTh1 ↓ ETTh1	96	0.380	0.412	0.382	0.397	0.375	0.399	0.367	0.398
	192	0.416	0.434	0.418	0.418	0.413	0.422	0.396	0.421
	336	0.448	0.458	0.437	0.434	0.434	0.438	0.471	0.437
	720	0.481	0.487	0.459	0.469	0.467	0.475	0.454	0.463
	Avg	0.431	0.448	0.424	0.430	0.422	0.434	0.422	0.430
ETTh2 ↓ ETTh1	96	0.380	0.412	0.388	0.418	0.384	0.415	0.388	0.421
	192	0.416	0.434	0.429	0.444	0.423	0.439	0.419	0.423
	336	0.448	0.458	0.467	0.472	0.458	0.465	0.435	0.444
	720	0.481	0.487	0.521	0.507	0.501	0.497	0.468	0.474
	Avg	0.431	0.448	0.451	0.460	0.441	0.454	0.428	0.441
Weather ↓ ETTh1	96	0.380	0.412	0.385	0.400	0.394	0.406	0.477	0.444
	192	0.416	0.434	0.417	0.429	0.425	0.424	0.454	0.522
	336	0.448	0.458	0.434	0.434	0.441	0.439	0.424	0.434
	720	0.481	0.487	0.444	0.464	0.446	0.468	0.468	0.469
	Avg	0.431	0.448	0.420	0.432	0.427	0.434	0.456	0.467
ETTh1 ↓ ETTh1	96	0.295	0.346	0.286	0.341	0.290	0.346	0.290	0.348
	192	0.333	0.374	0.322	0.362	0.353	0.388	0.327	0.372
	336	0.370	0.398	0.362	0.418	0.362	0.412	0.357	0.392
	720	0.427	0.431	0.417	0.431	0.422	0.432	0.409	0.423
	Avg	0.356	0.387	0.347	0.388	0.357	0.395	0.346	0.384
ETTh2 ↓ ETTh1	96	0.295	0.346	0.299	0.348	0.301	0.352	0.322	0.347
	192	0.333	0.374	0.324	0.366	0.332	0.359	0.332	0.372
	336	0.370	0.398	0.374	0.401	0.389	0.382	0.394	0.391
	720	0.427	0.431	0.415	0.419	0.421	0.442	0.411	0.424
	Avg	0.356	0.387	0.353	0.386	0.361	0.384	0.365	0.384
ETTh2 ↓ ETTh1	96	0.295	0.346	0.299	0.351	0.285	0.336	0.297	0.348
	192	0.333	0.374	0.334	0.372	0.343	0.366	0.332	0.370
	336	0.370	0.398	0.362	0.388	0.360	0.399	0.364	0.393
	720	0.427	0.431	0.417	0.431	0.422	0.432	0.410	0.421
	Avg	0.356	0.387	0.353	0.386	0.353	0.383	0.351	0.383
Weather ↓ ETTh1	96	0.295	0.346	0.322	0.361	0.309	0.354	0.294	0.354
	192	0.333	0.374	0.344	0.378	0.343	0.365	0.318	0.355
	336	0.370	0.398	0.371	0.399	0.401	0.411	0.361	0.397
	720	0.427	0.431	0.426	0.422	0.425	0.427	0.427	0.426
	Avg	0.356	0.387	0.366	0.390	0.370	0.389	0.350	0.383

Table 15: Full results for applying SimMTM to four advanced time series forecasting models under the in-domain setting. The gray mark represents negative transfer (↓).

Models	Transformer [16]				Autoformer [21]				Ns Transformer [10]				PatchTST [11]						
	Random init.		+SimMTM		Random init.		+SimMTM		Random init.		+SimMTM		Random init. +Sub-serie Masking		+SimMTM				
Metric	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	
ETTh1	96	0.847	0.731	0.775	0.691	0.536	0.548	0.526	0.536	0.513	0.491	0.490	0.489	0.375	0.399	0.366	0.398	0.373	0.399
	192	1.084	0.841	0.918	0.763	0.543	0.551	0.523	0.548	0.534	0.504	0.517	0.499	0.414	0.421	0.431	0.443	0.406	0.428
	336	1.350	0.956	1.079	0.845	0.615	0.592	0.595	0.591	0.588	0.535	0.552	0.520	0.431	0.436	0.450↓	0.456↓	0.422	0.431
	720	1.069	0.817	0.935	0.761	0.599	0.600	0.600	0.597	0.643	0.616	0.614	0.598	0.449	0.466	0.472↓	0.484↓	0.436	0.452
	Avg	1.088	0.836	0.927	0.761	0.573	0.573	0.561	0.568	0.570	0.537	0.543	0.527	0.417	0.431	0.430↓	0.445↓	0.409	0.428
ETTh2	96	2.029	1.150	1.879	1.104	0.492	0.517	0.488	0.514	0.476	0.458	0.445	0.448	0.274	0.336	0.284↓	0.343↓	0.274	0.337
	192	6.785	2.099	5.054	1.771	0.556	0.551	0.547	0.549	0.512	0.493	0.482	0.502	0.339	0.379	0.355↓	0.387↓	0.339	0.377
	336	4.568	1.711	4.242	1.658	0.572	0.578	0.563	0.570	0.552	0.551	0.512	0.537	0.331	0.380	0.379↓	0.411↓	0.327	0.381
	720	3.030	1.486	2.815	1.413	0.580	0.588	0.575	0.588	0.562	0.560	0.531	0.568	0.379	0.422	0.400↓	0.435↓	0.375	0.423
	Avg	4.103	1.612	3.498	1.487	0.550	0.559	0.543	0.555	0.526	0.516	0.493	0.514	0.331	0.379	0.355↓	0.394↓	0.329	0.379
ETTh1	96	0.562	0.520	0.513	0.497	0.523	0.488	0.482	0.465	0.386	0.398	0.340	0.376	0.290	0.342	0.289↓	0.344↓	0.288	0.343
	192	0.810	0.668	0.686	0.606	0.543	0.498	0.499	0.476	0.459	0.444	0.423	0.445	0.332	0.369	0.323	0.368	0.329	0.367
	336	1.096	0.814	1.003	0.760	0.675	0.551	0.601	0.524	0.495	0.464	0.423	0.459	0.366	0.392	0.353	0.387	0.361	0.387
	720	1.136	0.813	1.032	0.790	0.720	0.528	0.629	0.555	0.585	0.516	0.539	0.499	0.420	0.424	0.398	0.416	0.413	0.417
	Avg	0.901	0.704	0.809	0.663	0.615	0.528	0.553	0.505	0.481	0.456	0.431	0.445	0.352	0.382	0.341	0.379	0.348	0.378
ETTh2	96	0.508	0.539	0.336	0.425	0.255	0.339	0.255	0.340	0.192	0.274	0.188	0.277	0.165	0.255	0.166↓	0.256↓	0.163	0.253
	192	0.972	0.721	0.713	0.610	0.281	0.340	0.276	0.332	0.280	0.339	0.277	0.336	0.220	0.292	0.221↓	0.295↓	0.219	0.292
	336	1.419	0.897	1.517	0.942	0.339	0.372	0.309	0.359	0.334	0.361	0.325	0.355	0.278	0.329	0.278	0.333↓	0.275	0.328
	720	3.598	1.445	2.720	1.254	0.422	0.419	0.420	0.410	0.417	0.413	0.414	0.412	0.367	0.385	0.365	0.388↓	0.359	0.381
	Avg	1.624	0.901	1.322	0.808	0.324	0.368	0.315	0.360	0.306	0.347	0.301	0.345	0.258	0.317	0.258	0.318↓	0.254	0.313

Table 16: Full results for fine-tuning to limited data scenarios. We fine-tune the model pre-trained from ETTh2 to ETTh1 with different data proportions {10%, 25%, 50%, 75%, 100%}.

Models	SimMTM	Random init.	Ti-MAE[8]	TST[24]	LaST[17]	TF-C[25]	CoST[20]	TS2Vec[23]	
Metric	MSE MAE	MSE MAE	MSE MAE	MSE MAE	MSE MAE	MSE MAE	MSE MAE	MSE MAE	
ETTh2	10%	0.591 0.523	0.653 0.558	0.660 0.517	0.783 0.588	0.645 0.507	0.799 0.783	0.784 0.604	0.655 0.550
	25%	0.535 0.490	0.632 0.502	0.594 0.518	0.641 0.578	0.610 0.611	0.736 0.725	0.624 0.539	0.632 0.543
ETTh1	↓ 50%	0.491 0.473	0.512 0.479	0.550 0.504	0.525 0.509	0.540 0.513	0.731 0.704	0.540 0.499	0.599 0.526
	75%	0.466 0.458	0.499 0.488	0.475 0.465	0.516 0.488	0.479 0.470	0.697 0.689	0.494 0.475	0.577 0.534
	100%	0.415 0.430	0.431 0.448	0.466 0.456	0.469 0.459	0.443 0.471	0.635 0.634	0.428 0.433	0.517 0.486

Table 17: In- and cross-domain settings of classification, where **all the baselines are based on the encoder utilized in their original papers**. For in-domain setting, we pre-train and fine-tune on the same dataset: Epilepsy. For cross-domain setting, we pre-train the model on SleepEEG and then fine-tune it on different datasets: Epilepsy, FD-B, Gesture, and EMG.

Scenarios	Models	Accuracy (%)	Precision (%)	Recall (%)	F1 (%)	Avg (%)	
In-Domain		Random init.	89.83	92.13	74.47	79.59	84.00
	Epilepsy	TS2vec [23]	92.17	93.84	81.19	85.71	88.23
		CoST[20]	88.07	91.58	66.05	69.11	78.70
	Epilepsy	LaST [17]	92.11	93.12	81.47	85.74	88.11
		TST [24]	80.21	40.11	50.00	44.51	53.71
		Ti-MAE [8]	90.09	93.90	77.24	78.21	84.86
		TF-C [25]	93.96	94.87	85.82	89.46	91.03
		SimMTM	94.75	95.60	89.93	91.41	92.92
Cross-Domain		Random init.	89.83	92.13	74.47	79.59	84.00
	SleepEEG	TS2vec [23]	93.95	90.59	90.39	90.45	91.35
		CoST[20]	88.40	88.20	72.34	76.88	81.45
	Epilepsy	LaST [17]	86.46	90.77	66.35	70.67	78.56
		TST [24]	80.21	40.11	50.00	44.51	53.71
		Ti-MAE [8]	89.71	72.36	67.47	68.55	74.52
		TF-C [25]	94.95	94.56	89.08	91.49	92.52
		SimMTM	95.49	93.36	92.28	92.81	93.49
		Random init.	47.36	48.29	52.35	49.11	49.28
	SleepEEG	TS2vec [23]	47.90	43.39	48.42	43.89	45.90
		CoST[20]	47.06	38.79	38.42	34.79	39.76
	FD-B	LaST [17]	46.67	43.90	47.71	45.17	45.86
		TST [24]	46.40	41.58	45.50	41.34	43.71
		Ti-MAE [8]	60.88	66.98	68.94	66.56	65.84
	TF-C [25]	69.38	75.59	72.02	74.87	72.97	
	SimMTM	69.40	74.18	76.41	75.11	73.78	
	Random init.	42.19	47.51	49.63	48.86	47.05	
SleepEEG	TS2vec [23]	69.17	65.45	68.54	65.70	67.22	
	CoST[20]	68.33	65.30	68.33	66.42	67.09	
Gesture	LaST [17]	64.17	70.36	64.17	58.76	64.37	
	TST [24]	69.17	66.60	69.17	66.01	67.74	
	Ti-MAE [8]	71.88	70.35	76.75	68.37	71.84	
	TF-C [25]	76.42	77.31	74.29	75.72	75.94	
	SimMTM	80.00	79.03	80.00	78.67	79.43	
	Random init.	77.80	59.09	66.67	62.38	66.49	
SleepEEG	TS2vec [23]	78.54	80.40	67.85	67.66	73.61	
	CoST[20]	53.65	49.07	42.10	35.27	45.02	
EMG	LaST [17]	66.34	79.34	63.33	72.55	70.39	
	TST [24]	78.34	77.11	80.30	68.89	76.16	
	Ti-MAE [8]	69.99	70.25	63.44	70.89	68.64	
	TF-C [25]	81.71	72.65	81.59	76.83	78.20	
	SimMTM	97.56	98.33	98.04	98.14	98.02	

Table 18: In- and cross-domain settings of classification **based on the unified 1-D ResNet encoder**. For in-domain setting, we pre-train and fine-tune on the same dataset: Epilepsy. For cross-domain setting, we pre-train on SleepEEG and fine-tune on different domain datasets: Epilepsy, FD-B, Gesture, and EMG.

Scenarios	Models	Accuracy (%)	Precision (%)	Recall (%)	F1 (%)	Avg (%)	
In-Domain	Epilepsy ↓ Epilepsy	Random init.	89.83	92.13	74.47	79.59	84.00
		TS2vec [23]	92.33	94.53	81.11	86.33	88.58
		CoST[20]	92.35	94.73	81.16	85.92	88.54
		LaST [17]	-	-	-	-	-
		TST [24]	80.89	90.38	51.73	48.01	67.75
		Ti-MAE [8]	80.34	90.16	50.33	45.20	66.51
		TF-C [25]	93.96	94.87	85.82	89.46	91.03
		SimMTM	94.75	95.60	89.93	91.41	92.92
Cross-Domain	SleepEEG ↓ Epilepsy	Random init.	89.83	92.13	74.47	79.59	84.00
		TS2vec [23]	94.46	91.99	90.28	91.10	91.95
		CoST[20]	93.66	91.39	88.08	89.60	90.68
		LaST [17]	-	-	-	-	-
		TST [24]	82.89	86.15	79.02	80.44	82.13
		Ti-MAE [8]	73.45	72.56	65.34	77.20	72.14
		TF-C [25]	94.95	94.56	89.08	91.49	92.52
		SimMTM	95.49	93.36	92.28	92.81	93.49
	SleepEEG ↓ FD-B	Random init.	47.36	48.29	52.35	49.11	49.28
		TS2vec [23]	60.74	59.60	64.27	61.07	61.42
		CoST[20]	54.82	51.92	63.30	54.34	56.09
		LaST [17]	-	-	-	-	-
		TST [24]	65.57	70.05	67.57	64.41	66.90
		Ti-MAE [8]	67.98	62.83	64.45	63.36	64.66
		TF-C [25]	69.38	75.59	72.02	74.87	72.97
SimMTM		69.40	74.18	76.41	75.11	73.78	
SleepEEG ↓ Gesture	Random Init.	42.19	47.51	49.63	48.86	47.05	
	TS2vec [23]	73.33	70.88	73.33	71.56	72.27	
	CoST[20]	73.33	74.37	73.33	71.16	73.04	
	LaST [17]	-	-	-	-	-	
	TST [24]	75.12	76.05	67.74	73.24	73.04	
	Ti-MAE [8]	75.54	69.32	72.42	69.32	71.65	
	TF-C [25]	76.42	77.31	74.29	75.72	75.94	
	SimMTM	80.00	79.03	80.00	78.67	79.43	
SleepEEG ↓ EMG	Random init.	77.80	59.09	66.67	62.38	66.49	
	TS2vec [23]	80.92	69.63	67.65	67.90	71.52	
	CoST[20]	73.17	70.47	69.84	70.00	70.87	
	LaST [17]	-	-	-	-	-	
	TST [24]	75.89	74.67	80.66	78.48	77.43	
	Ti-MAE [8]	63.52	67.77	70.55	58.32	65.04	
	TF-C [25]	81.71	72.65	81.59	76.83	78.20	
	SimMTM	97.56	98.33	98.04	98.14	98.02	

Table 19: Full ablation studies for in-domain and cross-domain settings of classification. Under the Avg metric, the standard deviations of SimMTM are within 0.2% for Epilepsy, within 0.5% for FD-B, within 0.6% for Gesture, and within 0.1% for EMG.

Scenarios		Accuracy (%)	Precision (%)	Recall (%)	F1 (%)	Avg (%)
Epilepsy ↓ Epilepsy	Random init.	89.83	92.13	74.47	79.59	84.00
	W/o $\mathcal{L}_{\text{reconstruction}}$	93.80	96.11	86.11	89.45	91.37
	W/o $\mathcal{L}_{\text{constraint}}$	90.99	92.81	79.86	84.13	86.95
	SimMTM	94.75	95.60	89.93	91.41	92.92
SleepEEG ↓ Epilepsy	Random init.	89.83	92.13	74.47	79.59	84.00
	W/o $\mathcal{L}_{\text{reconstruction}}$	94.54	93.87	88.46	90.84	91.93
	W/o $\mathcal{L}_{\text{constraint}}$	91.73	90.57	82.21	85.53	87.51
	SimMTM	95.49	93.36	92.28	92.81	93.49
SleepEEG ↓ FD-B	Random init.	47.36	48.29	52.35	49.11	49.28
	W/o $\mathcal{L}_{\text{reconstruction}}$	66.11	67.97	74.70	70.01	69.70
	W/o $\mathcal{L}_{\text{constraint}}$	53.71	69.48	62.67	50.86	59.18
	SimMTM	69.40	74.18	76.41	75.11	73.78
SleepEEG ↓ Gesture	Random init.	42.19	47.51	49.63	48.86	47.05
	W/o $\mathcal{L}_{\text{reconstruction}}$	78.50	79.01	78.50	77.17	78.30
	W/o $\mathcal{L}_{\text{constraint}}$	76.67	74.91	76.67	74.80	75.76
	SimMTM	80.00	79.03	80.00	78.67	79.43
SleepEEG ↓ EMG	Random init.	77.80	59.09	66.67	62.38	66.49
	W/o $\mathcal{L}_{\text{reconstruction}}$	90.24	94.20	78.04	81.53	86.00
	W/o $\mathcal{L}_{\text{constraint}}$	85.37	89.97	69.62	70.74	78.93
	SimMTM	97.56	98.33	98.04	98.14	98.02

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