# CBD: A Certified Backdoor Detector Based on Local Dominant Probability

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## Abstract

Backdoor attack is a common threat to deep neural networks. During testing, samples embedded with a backdoor trigger will be misclassified as an adversarial target by a backdoored model, while samples without the backdoor trigger will be correctly classified. In this paper, we present the first certified backdoor detector (CBD), which is based on a novel, adjustable conformal prediction scheme based on our proposed statistic *local dominant probability*. For any classifier under inspection, CBD provides 1) a detection inference, 2) the condition under which the attacks are guaranteed to be detectable for the same classification domain, and 3) a probabilistic upper bound for the false positive rate. Our theoretical results show that attacks with triggers that are more resilient to test-time noise and have smaller perturbation magnitudes are more likely to be detected with guarantees. Moreover, we conduct extensive experiments on four benchmark datasets considering various backdoor types, such as BadNet, CB, and Blend. CBD achieves comparable or even higher detection accuracy than state-of-the-art detectors, and it in addition provides detection certification. Notably, for backdoor attacks with random perturbation triggers bounded by  $\ell_2 \leq 0.75$  which achieves more than 90% attack success rate, CBD achieves 100% (98%), 100% (84%), 98% (98%), and 72% (40%) empirical (certified) detection true positive rates on the four benchmark datasets GTSRB, SVHN, CIFAR-10, and TinyImageNet, respectively, with low false positive rates.

# **1** Introduction

Despite the success of deep neural networks (DNNs) in many applications, they are vulnerable to adversarial attacks such as backdoor attacks [46, 36]. A DNN being backdoored will learn to predict an adversarial target class for test samples embedded with a backdoor trigger, while maintaining a high accuracy on clean test samples without the trigger [18, 8, 42, 65, 50, 43, 51, 37].

Backdoor detection is a popular task for backdoor defense. It aims to detect if a given model is backdoored without access to the training set or any real test samples that are possibly embedded with the trigger [48, 64]. The task corresponds to practical scenarios where the user of an app or a legacy system containing a DNN seeks to know if the model is backdoor attacked, where the training set is not available [1]. Various empirical approaches have been proposed for backdoor detection, most of which are based on trigger reverse engineering [67, 6, 75, 69, 56, 62, 24], or meta classification [82, 29]. However, none of these works quantitatively investigate the conditions under which the backdoor attacks are guaranteed to be detectable. Without a detection guarantee, DNNs are still vulnerable to future attacks (e.g.) with new trigger types [51, 87, 70].

In this paper, we make the first attempt toward the *certification* of backdoor detection. Certification is an important concept for studies on the robustness of DNNs against adversarial examples [61, 17, 52, 7, 45]. In particular, a robustness certification refers to a probabilistic or deterministic guarantee for a model to produce desired outputs (e.g. correct label prediction) when the adversarial perturbation applied to the inputs satisfies certain conditions (e.g. with some constrained perturbation magnitude) [33, 58, 32, 10, 59]. As an analogy, we propose a *certified backdoor detector* (CBD)

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that is guaranteed to trigger an alarm if the attack for a given domain satisfies certain conditions. In Sec. 3, we introduce the detection procedure of CBD based on conformal prediction (with our proposed, optional adjustment scheme) using a novel (model-level) statistic named *local dominant probability*. The calibration set for conformal prediction is obtained from a small number of benign shadow models trained on a small validation set, which addresses the unavailability of the training set. In Sec. 4, we derive the condition for attacks with detection guarantee, as well as a probabilistic upper bound for the false positive rate of our detector, for any prescribed significance level specifying the aggressiveness of the detection. Notably, our certification is comprehensive – for any domain, more effective attacks with strong *trigger robustness* (which measures the resilience of a trigger against test-time noises) and more stealthy attacks (against human inspectors) with small trigger perturbation magnitudes are easier to be detected with guarantees. Moreover, both our detector and the certification method do not assume the trigger incorporation mechanism or the training configuration of the model, which allows their potential application to future attacks. Our contributions are summarized below:

- We propose CBD, the first certified backdoor detector, which is based on an adjustable conformal prediction scheme using a novel *local dominant probability* statistic.
- We propose a certification method and show that for any domain, backdoor attacks with stronger *trigger robustness* and smaller trigger perturbation magnitudes are more likely to be detected by CBD with guarantee. We also derive a probabilistic upper bound for the false positive rate of CBD.
- We show that CBD achieves comparable or even higher detection accuracy than state-of-the-art detectors against three types of backdoors. We also show that for backdoor attacks with random perturbation triggers bounded by  $\ell_2 \leq 0.75$ , CBD achieves 100% (98%), 100% (84%), 98% (98%), and 72% (40%) empirical (certified) true positive rates on GTSRB, SVHN, CIFAR-10, and TinyImageNet, respectively, with only 0%, 0%, 6%, and 10% false positive rates, respectively.

# 2 Related Work

**Backdoor Detection Methods** Existing methods for backdoor detection are all empirical without theoretical guarantees. An important type of reverse-engineering-based method estimates putative triggers for anomaly detection [67, 6, 75, 41, 78, 73, 79, 76, 69, 56, 62, 24]. Certification for these methods is hard due to the complexity of trigger reverse engineering. Another type of detector is based on meta-classification that involves a large number of shadow models trained with and without attacks [82, 29]. Differently, our CBD is based on conformal prediction involving a scalar detection statistic (rather than a high dimensional feature vector employed by [82, 29]), such that only a small number of benign shadow models will be required. More importantly, our CBD is certified, i.e. with a detection guarantee, which is different from all the detention methods mentioned above.

**Other Backdoor Defense Tasks** Backdoor defenses during training aim to produce a backdoor-free classifier from the possibly poisoned training set [63, 5, 74, 14, 25, 57, 77, 23, 4, 16]. These defenses require access to the training set, which is unavailable for backdoor detection. Backdoor mitigation aims to "repair" models being backdoor attacked [40, 72, 35, 19, 88, 85], which can be viewed as a downstream task following backdoor detection. Inference-stage trigger detection aims to detect if a test sample contains the trigger [15, 55, 12, 9, 44, 34]. However, backdoor detection is performed before the inference stage, where test samples are not available. These defense tasks will not be further discussed due to their fundamental differences from the backdoor detection task.

**Certified Backdoor Defenses** Existing methods mostly modify the training process to prevent the backdoor from being learned, while manipulating the test sample to destroy any potentially embedded triggers [86, 71, 27, 53]. These methods are not applicable to the backdoor detection problem where both the training set and the test samples are not available. More importantly, all these existing certified defenses are deployed during training, which requires an uncontaminated training process fully controlled by the defender. In contrast, in this paper, we consider a stronger threat model that allows the attacker to have full control of the training process.

## **3** Detection Method

#### 3.1 **Problem Definition**

**Threat Model** Consider a classification domain with sample space  $\mathcal{X}$  and label space  $\mathcal{Y}$ . A backdoor attack is specified by a trigger with some incorporation function  $\delta : \mathcal{X} \to \mathcal{X}$  and a target class  $t \in \mathcal{Y}$ . For a successful backdoor attack, the victim classifier will predict to the target class t whenever a

test sample is embedded with the trigger, while test samples without the trigger will be correctly classified [18, 8, 42, 38]. In this paper, we do allow advanced attackers with full control of the training process [51, 87, 70, 50, 3]. This is deemed a stronger threat model than all previous works on certified backdoor defense where the defender is assumed with full control of the training process. However, in this paper, we do not consider backdoor attacks with multiple triggers or target classes [84, 83] – even empirical detection of these attacks is a challenging problem [80].

**Goal of Certified Backdoor Detection** The fundamental goal is backdoor detection, i.e. to infer if a given classifier  $f(\cdot; w) : \mathcal{X} \to \mathcal{Y}$  is backdoored or not [48, 64]. The defender has no access to the training set or any test samples that may contain the trigger. In practice, the defender also has no access to benign classifiers with high accuracy for the same domain as  $f(\cdot; w)$  – otherwise, these benign classifiers can be used for the task, and detection will be unnecessary. However, the defender is assumed with a small validation set of clean samples for detection – this is a standard assumption made by most post-training backdoor defenses [67, 82, 75, 56, 41].

Beyond model inference, a *certified* backdoor detector also needs to provide each classification domain (associated with the model to be inspected) with a condition on  $\delta$ , t, and w, such that any successful backdoor attack with a trigger  $\delta$  and a target class t on a victim classifier  $f(\cdot; w)$  (trained on this classification domain) is guaranteed to be detected if the condition is satisfied. The stronger a certification is, the more likely a successful attack on the domain will be detectable with guarantee. Moreover, a certification has to be associated with a guarantee on the false positive rate; otherwise, an arbitrarily strong certification can be achieved by increasing the aggressiveness of the detection rule.

#### **3.2** Overview of CBD Detection

Key Intuition For a successful backdoor attack with a trigger  $\delta$  and a target class t, a test instance x embedded with the trigger (denoted by  $\delta(x)$ ) will be classified to the target class t with high probability. Practical backdoor triggers should also be robust (i.e. resilient) to noises either from the environment or introduced by simple defenses based on input-preprocessing such as blurring and/or quantization [81, 39]. Such *trigger robustness* can be measured by the distribution of the model prediction in the neighborhood of each  $\delta(x)$  – the more robust the trigger is, the more samples in the neighborhood of  $\delta(x)$  will be predicted to the target class t. Thus, if the perturbation magnitude of a robust trigger, i.e.  $||\delta(x) - x||_2$ , is small (which is usual for backdoor attacks to achieve stealthiness), a significant proportion of samples in the neighborhood of x will also be classified to class t due to their closeness to  $\delta(x)$ . Such an increment in the target class probability in the neighborhood of all instances is captured by our proposed statistic named *local dominant probability* (LDP) to distinguish backdoored classifiers from benign ones – the former tend to have a larger LDP than the latter.

**Outline of CBD Detection Procedure** In short, CBD performs an *adjustable* conformal prediction to test if the LDP statistic computed for the model to be inspected is sufficiently large to trigger an alarm. A small number of shadow models (with the same architecture as the model to be inspected) are trained on a relatively small validation set, with an LDP computed for each shadow model to form a calibration set. Then, a small proportion of outliers with large values in the calibration set are optionally removed, e.g., by anomaly detection. Based on this adjusted calibration set, the p-value is computed for the LDP for the model to be inspected. The model is deemed to be backdoored if the p-value is less than some prescribed significance level (e.g. the classical 0.05 for statistical testing).

#### 3.3 Definition of LDP

We first define a *samplewise local probability vector* (SLPV) to represent the distribution of the model prediction outcomes in the neighborhood of any given sample. Then, based on SLPV, we define the *samplewise trigger robustness* (STR) that measures the resilience of a trigger to the Gaussian noise when it is embedded in a particular sample. Finally, we define the LDP statistic based on SLPV.

**Definition 3.1.** (*Samplewise Local Probability Vector (SLPV*)) For any classifier  $f(\cdot; w) : \mathcal{X} \to \mathcal{Y}$ with parameters w, the SLPV for any input  $x \in \mathcal{X}$  is a probability vector  $\mathbf{p}(x|w, \sigma) \in [0, 1]^K$  over the  $K = |\mathcal{Y}|$  classes, with the k-th entry defined by  $p_k(x|w, \sigma) \triangleq \mathbb{P}_{\epsilon \sim \mathcal{N}(0,\sigma^2 I)}(f(x + \epsilon; w) = k)$ ,  $\forall k \in \mathcal{Y}$ , where  $\mathcal{N}(\mu, \Sigma)$  represents Gaussian distribution with mean  $\mu$  and covariance  $\Sigma$ .

**Remarks:** If  $f(\cdot; w)$  is continuous at x with f(x; w) = k for some  $k \in \mathcal{Y}$ , it is trivial to show that  $p_k(x|w, \sigma) \to 1$  as  $\sigma \to 0$ , i.e. the SLPV becomes a singleton at the predicted class of x without the Gaussian noise. In practice, SLPV can be estimated by Monte Carlo for any given model and sample.



(a) Benign classifier with a small LDP close to  $\frac{1}{4}$ .



(b) Classifier being backdoored with a large LDP.

Figure 1: Illustration of the difference in LDP between benign and backdoored classifiers on a classification domain with K = 4 classes. A backdoor attack with a robust trigger  $\delta$  (with a small perturbation magnitude) and a target class 4 (with orange decision region) changes the class distribution in the neighborhood of  $x_1$ ,  $x_2$ , and  $x_3$ , resulting in a larger LDP for the backdoored model than for the benign model.

**Definition 3.2.** (Samplewise Trigger Robustness (STR)) Consider a backdoor attack with a trigger  $\delta$  and a target class  $t \in \mathcal{Y}$  against a victim model  $f(\cdot; w)$ . For any sample  $x \in \mathcal{X}$  and any isotropic Gaussian distribution  $\mathcal{N}(0, \sigma^2 I)$ , the STR is defined by the t-th entry of the SLPV for  $\delta(x)$  (i.e. sample x with the trigger  $\delta$  embedded), which is denoted by  $R_{\delta,t}(x|w, \sigma) \triangleq p_t(\delta(x)|w, \sigma)$ .

**Remarks:** STR measures the resilience of a trigger against Gaussian noises. Usually, strong STR can be naturally achieved by embedding the trigger in a large variety of samples during training.

**Definition 3.3.** (*Local Dominant Probability (LDP*)) Consider a domain with  $K = |\mathcal{Y}|$  classes and an isotropic Gaussian distribution  $\mathcal{N}(0, \sigma^2 I)$ . The LDP for a classifier  $f(\cdot; w)$  is defined by

$$s(w) = \left|\left|\frac{1}{K}\sum_{k=1}^{K} \boldsymbol{p}(x_k|w,\sigma)\right|\right|_{\infty}$$
(1)

where  $x_1, \dots, x_K$  are K independent random samples satisfying  $f(X_k; w) = k, \forall k \in \{1, \dots, K\}$ .

**Remarks:** By the definition, LDP for a given classifier  $f(\cdot; w)$  is computed on  $x_1, \dots, x_K$  independently sampled from the K classes respectively, satisfying  $f(x_k; w) = k$  for  $\forall k$ . LDP computed on more samples per class yields similar detection and certification performance empirically. Specifically, we first compute the SLPV for each of the K samples. Then we take the average of the K SLPVs and pick the maximum entry as the LDP for  $f(\cdot; w)$ . Note that LDP is always no less than  $\frac{1}{K}$ .

As stated in the key intuitions in Sec. 3.2, LDP tends to be larger for backdoored classifiers than for benign ones. This can be understood from the illustration in Fig. 1 for a classification domain with K = 4 classes. For the benign classifier on the left, the SLPVs for  $x_1, \dots, x_4$  are almost orthogonal to each other, leading to a small LDP close to  $\frac{1}{4}$ . On the right, we consider a backdoor attack with a robust trigger  $\delta$  and a target class 4 (with orange decision region). The strong STRs for  $x_1, x_2$ , and  $x_3$  (represented by the large orange regions around  $\delta(x_1), \delta(x_2)$ , and  $\delta(x_3)$ ), together with the small trigger perturbation magnitudes (i.e. small  $||\delta(x_i) - x_i||_2$  for i = 1, 2, 3), significantly change the class distribution in the neighborhood of each of  $x_1, x_2$ , and  $x_3$ . In particular, there will be a clear increment in the 4-th entry of the SLPVs for  $x_1, x_2$ , and  $x_3$ . Thus, the 4-th entry associated with the backdoor target class will dominate the average SLPV over  $x_1, \dots, x_4$ , leading to a large LDP.

### 3.4 CBD Detection Procedure

Although backdoored and benign classifiers have different LDP distributions, it is still a challenge in practice to set a detection threshold. To solve this problem, we propose to use the conformal prediction, which employs a calibration set for supervision [66, 2]. Here, the calibration set consists of LDP statistics obtained from a small number of benign shadow models trained on the small validation set possessed by the defender. However, the actual benign classifiers to be inspected are usually trained on more abundant data, such that the LDPs for these classifiers will likely follow a different distribution from the LDPs for the shadow models without sufficient training. In particular, the LDPs in the calibration set (obtained from the shadow models) may easily have an overly large sample variance and a heavy tail of large outliers. Directly using this calibration set for conformal prediction may lead to a conservative detection due to an overly large detection threshold.

Thus, we propose an optional adjustment scheme that treats the m largest LDP statistics in the calibration set as outliers. In practice, prior knowledge may be required to determine the exact value

of *m*, while in our experiments, a small  $m/N \le 0.2$ , where *N* is the size of the calibration set) may significantly increase the detection or certification power of our CBD with only small increment to the false positive rate. The detection procedure of our CBD consists of the following four steps: 1) Given a classifier  $f(\cdot; w)$  to be inspected, estimate LDP s(w) based on Def. 3.3.

2) Train (benign) shadow models  $f(\cdot; w_1), \dots, f(\cdot; w_N)$  on the clean validation dataset, and construct a calibration set  $S_N = \{s(w_1), \dots, s(w_N)\}$  by computing the LDP for each model. 3) Compute the adjusted conformal p-value (assuming *m* large outliers) defined by:

$$q_m(w) = 1 - \frac{1 + \min\{|\{s \in \mathcal{S}_N : s < s(w)\}|, N - m\}}{N - m + 1}$$
(2)

4) Trigger an alarm if  $q_m(w) \leq \alpha$ , where  $\alpha$  is a prescribed significance level (e.g.  $\alpha$ =0.05).

# 4 CBD Certification

In addition to a detection inference, CBD also provides a certification, which is a condition under which attacks are guaranteed to be detectable. Detailed proofs in this section are shown in App. A.

**Theorem 4.1.** (Backdoor Detection Guarantee) For an arbitrary classifier  $f(\cdot; w) : \mathcal{X} \to \mathcal{Y}$  to be inspected, let  $x_1, \dots, x_K$  be the K randomly selected samples and  $\mathcal{N}(0, \sigma^2 I)$  be the isotropic Gaussian distribution used to compute the LDP for  $f(\cdot; w)$ . Let  $\alpha$  be the prescribed significance level of CBD. A backdoor attack with a trigger  $\delta$  and a target class t is guaranteed to be detected if:

$$\Delta < \sigma(\Phi^{-1}(1 - s_{(N-m-\lfloor \alpha(N-m+1) \rfloor)}) - \Phi^{-1}(1-\pi))$$
(3)

where  $\Phi$  is the standard Gaussian CDF,  $\pi = \min_{k=1,\dots,K} R_{\delta,t}(x_k|w,\sigma)$  is the minimum STR over  $x_1, \dots, x_K$ ,  $\Delta = \max_{k=1,\dots,K} ||\delta(x_k) - x_k||_2$  is the maximum perturbation magnitude of the trigger, m is the number of assumed outliers in the calibration set  $S_N$  with size N, and  $s_{(n)}$  denotes the n-th smallest element in  $S_N$ .

*Proof (sketch).* The STR for each sample  $x_k$  equals the *t*-th entry of the SLPV for  $\delta(x_k)$  by Def. 3.2. We also connect the SLPV for  $\delta(x_k)$  to the SLPV for  $x_k$  using the Neyman-Pearson lemma ([49]). Based on this connection, we derive the lower bound for the minimum STR, such that the *t*-th entry of the SLPV of each  $x_k$  is sufficiently large to result in a large LDP for the attack to be detected.  $\Box$ 

**Remarks:** (1) (**Main Results**) For fixed trigger perturbation size ( $\Delta$ ), detection of attacks with larger STR ( $\pi$ ) is more likely to be guaranteed; while for fixed STR, detection of attacks with smaller trigger perturbation size is more likely to be guaranteed. (2) Our backdoor detection guarantee is inspired by the randomized smoothing approach in [10] for certified robustness against adversarial examples. However, certified backdoor detection and certified robustness against adversarial examples are fundamentally different, as will be detailed in App. I. (3) Certified backdoor detection guarantees to strong backdoor attacks, while the latter prevents the trigger from being learned during training [86, 53]. The two types of certification may cover the entire attack space together in the future, such that a backdoor attack will be either strong enough to be detected or weak enough to be disabled.

A meaningful certification for backdoor detection should also be along with a guarantee for the false positive rate (FPR). Otherwise, one can easily design a backdoor detector that always triggers an alarm, which provides detection guarantees to all backdoor attacks but is useless in practice.

**Theorem 4.2.** (Probabilistic Upper Bound for FPR) Consider a random calibration set  $S_N = \{s_1, \dots, s_N\}$  with  $s_1, \dots, s_N$  i.i.d. following some continuous distribution F. Consider a random benign classifier  $f(\cdot; W)$  with LDP s(W) following some distribution  $\tilde{F}$ . Assume F dominates  $\tilde{F}$  in the sense of first-order stochastic dominance. Let m be any number of assumed outliers in  $S_N$  and let  $\alpha$  be any prescribed significance level of CBD. Then, the FPR of CBD on  $f(\cdot; W)$  conditioned on  $S_N$ , which is denoted by  $Z_N = \mathbb{P}(q_m(W) \leq \alpha | S_N)$  based on Eq. (2), will be first-order dominated by a random variable B following Beta(m + l + 1, N - m - l) with  $l = \lfloor \alpha(N - m + 1) \rfloor$ , i.e.  $B \succeq_1 Z_N$ . In other words,  $\mathbb{P}(Z_N \leq q) \geq \mathbb{P}(B \leq q)$  for any real q.

*Proof (sketch).* We first express the false positive rate  $Z_N$  in terms of the order statistics on the elements of the random calibration set  $S_N$ . Then, we derive the lower bound of the CDF of  $Z_N$  using the distribution of order statistics followed by a binomial expansion.

**Remarks:** The assumption that F dominates  $\tilde{F}$  in Thm. 4.2 generally holds in practice. Again, this is because the actual benign classifiers to be inspected are usually trained on more abundant data than the benign shadow models. Empirical results supporting this assumption are shown in Sec. 5.4. Moreover, an analysis of this phenomenon is presented in App. B, where we show on binary Bayes classifiers that a higher empirical loss can easily lead to a larger expected LDP.

While we have shown that  $Z_N$  conditioned on a random calibration set of size N is upper bounded by a Beta random variable in the sense of first-order stochastic dominance, in Col. 4.3 below, we show that asymptotically, the upper bound of  $Z_N$  converges to a constant in probability as  $N \to \infty$ . **Corollary 4.3.** (Asymptotic Property of FPR) Consider the settings in Thm. 4.2. For any  $\xi > 0$ ,  $\lim_{N\to+\infty} \mathbb{P}(Z_N \leq \tau) = 1$ , where  $\tau = \alpha + (1 - \alpha)\beta + \xi$  with  $\beta = m/N$ .

*Proof (sketch).* We show that any random variable *B* with the Beta distribution described in Thm. 4.2 satisfies  $\lim_{N\to+\infty} \mathbb{P}(B \leq \tau) = 1$ . Then, the corollary is proved since  $Z_N$  is dominated by *B*.

**Remarks:** For classical conformal prediction without adjustment where m = 0, we will have  $\beta = 0$ and  $\lim_{N \to +\infty} \mathbb{P}(Z_N \leq \alpha + \xi) = 1$  for any  $\xi > 0$ . In this case, the upper bound of the false positive rate of our CBD converges to the prescribed significance level  $\alpha$  in probability.

# 5 Experiment

There have been many different types of backdoor attacks proposed, each also with a wide range of configurations. Thus, it is infeasible to evaluate our CBD over the entire space of backdoor attacks. Inspired by the evaluation protocol for certified robustness [10], in Sec. 5.1, we focus on backdoor attacks with random perturbation triggers to comprehensively evaluate the certification capability of our CBD. In Sec. 5.2, we compare CBD with three state-of-the-art backdoor detectors (all "uncertified") against backdoor attacks with three popular trigger types to evaluate the detection capability of CBD. In Sec. 5.3, we present ablation studies (e.g. on the number of shadow models used by CBD). Additional results and other supportive empirical analyses are shown in Sec. 5.4.

## 5.1 Evaluation of CBD Certification

For certified robustness, the prediction of a test example is unchanged with a guarantee, if the magnitude of the adversarial perturbation is smaller than the *certified radius* [10]. Certified robustness is usually evaluated by the *certified accuracy* on some random test set as the proportion of the samples that are guaranteed to be correctly classified if the magnitude of the adversarial perturbation is no larger than some prescribed value. As an analog, our certification for backdoor detection is specified by an inequality that involves both the STR and the perturbation magnitude of the trigger, which naturally produces a two-dimensional "*certified region*" (illustrated in Fig. 7 and Fig. 8 in Apdx. D). Our certification method is evaluated on a set of random backdoor attacks, each using a random pattern as the trigger, with the perturbation magnitude satisfying some  $\ell_2$  constraint. We are interested in the proportion of the attacks falling into the certified region, i.e. guaranteed to be detected.

## 5.1.1 Setup

**Dataset:** Our experiments are conducted on four benchmark image datasets, GTSRB [60], SVHN [47], CIFAR-10 [30], and TinyImageNet [11], following their standard train-test splits. Due to the large number of models that will be trained to evaluate our certification method, except for GTSRB, we use 40% of the training set to train these models. We also reserve 5,000 samples from the test set of GTSRB, SVHN, and CIFAR-10, and 10,000 samples from the test set of TinyImageNet (much smaller than the training size for the models for evaluation) for the defender to train the shadow models. More details about these datasets are deferred to App. C.1.

**Evaluation Metric:** Following the convention, the detection performance of CBD is evaluated by the true positive rate (**TPR**) defined by the proportion of attacks being detected (with a correct inference of the target class) and the false positive rate (**FPR**) defined by the proportion of benign classifiers falsely detected. For certification, we define certified TPR (**CTPR**) as the proportion of a set of attacks that are guaranteed to be detectable, i.e. falling into the certified region.

**Attack Setting:** For each dataset, we create 50 backdoor attacks, each with a randomly selected target class. For each attack, we generate a random trigger, which is a random perturbation embedded



Figure 2: Certification performance of CBD against backdoor attacks with random triggers with perturbation magnitude  $\ell_2 \leq 0.75$  measured by CTPR (solid) for a range of  $\sigma$  for  $\beta = 0, 0.1, 0.2$ . The CTPRs are all upper-bounded by the TPRs (dashed), showing the correctness of our certification. Notably, CBD achieves up to 98% (100%), 84% (100%), 98% (98%), and 40% (72%) CTPRs (TPRs) on GTSRB, SVHN, CIFAR-10, and TinyImageNet, respectively, across all choices of  $\sigma$  and  $\beta$ . An increment in  $\beta$ , the assumed ratio of calibration outliers, may lead to further increments in both CTPR and TPR. The hyperparameter  $\sigma$  can be determined using the calibration set in practice.

by  $\delta(x) = x + v$  with  $||v||_2 \le 0.75$ . The generation process also involves random nullification of the trigger pattern, which helps the trigger to be learned. More details about trigger generation are deferred to App. C.2 due to space limitations. The poisoning ratios for the attacks on GTSRB, SVHN, CIFAR-10, and TinyImageNet are 7.8%, 15.3%, 11.3%, and 12.4%, respectively. Lower poisoning ratios may largely reduce the attack success rate since many randomly generated triggers are relatively hard to learn. Results for triggers with larger perturbation size are shown in App. D.

**Training:** For model architecture, we use the winning model on the leaderboard [31] for GTSRB, MobileNetV2 [54] for SVHN, the same architecture in [82] for CIFAR-10, and ResNet-34 [22] for TinyImageNet. For each dataset, 50 benign models are trained (also on the 40% training set except for GTSRB) to evaluate the FPR. The accuracies for these benign models are roughly 98%, 92%, 78%, and 47% on GTSRB, SVHN, CIFAR-10, and TinyImageNet, respectively. For each attack, we train a model with  $\geq$  90% attack success rate and  $\leq$  2% degradation in the benign accuracy (or re-generate the attack for training until both conditions are satisfied). More details about the training configurations are shown in App. C.3. Finally, we train 100 shadow models for each of GTSRB, SVHN, and CIFAR-10, and 50 shadow models for TinyImageNet using the same architectures and configurations as above – these shadow models are used by our CBD for detection and certification.

### 5.1.2 Certification Performance

In Fig. 2, we show the CTPR (solid) of our CBD against the attacks with the random perturbation trigger on the four datasets for a range of  $\sigma$  and for  $\beta = m/N \in \{0, 0.1, 0.2\}$ . The TPR (dashed) for each combination of  $\sigma$  and  $\beta$  is also plotted for reference. Recall that  $\beta$  here represents the proportion of assumed outliers in the calibration set for the adjustment of the conformal prediction, and  $\sigma$  is the standard deviation of the isotropic Gaussian distribution for the LDP computation. In our experiments, 1024 random Gaussian noises are generated for each sample used to compute the LDP. The significance level for conformal prediction is set to the classical  $\alpha = 0.05$  for statistical testing.

In general, our certification is effective, which covers up to 98%, 84%, and 98% backdoor attacks with the random perturbation trigger (all achieved with  $\beta = 0.2$ ) on GTSRB, SVHN, and CIFAR-10, respectively. Even for the very challenging TinyImageNet dataset, CBD certifies up to 40% of these attacks. Moreover, for all choices of  $\beta$  and  $\sigma$ , CTPR is upper-bounded by TPR. For example, for the aforementioned CTPRs on the four datasets, the corresponding TPRs are 100%, 100%, 98%, and 72%, respectively (with FPRs 0%, 0%, 6%, and 10%, respectively, see App. D). In fact, all attacks with the detection guarantee are detected empirically, showing the correctness of our certification.

We also make the following observations regarding the hyperparameters  $\beta$  and  $\sigma$ : 1) An increment in  $\beta$  may lead to an increment in both CTPR and TPR. This is due to the existence of a heavy tail

(corresponding to large outliers) in the LDP distribution for the calibration set. While an overly large  $\beta$  may cause a significant increment to FPR, our additional results in App. D show that empirically, this is not the case for  $\beta \leq 0.2$ . 2) Each domain has its own proper range for the choice of  $\sigma$ . In general, the detection power of CBD (reflected by TPR) reduces as  $\sigma$  becomes overly small. This phenomenon agrees with our remarks on Def. 3.1 -SLPV converges to a singleton at the labeled class as  $\sigma$  approaches zero, regardless of the presence of a backdoor attack. Moreover, the certification power (reflected by CTPR) also reduces for small  $\sigma$ 's, which matches the inequality (3) in Thm. 4.1. For overly large  $\sigma$ 's, on the other hand, LDP for benign classifiers may also grow and possibly approach one, resulting in a large FPR. However, in this case, LDP is no longer computed in a truly 'local' context, contrary to the intuition implied by its name. In Sec. 5.2, we will introduce a practical scheme to choose a proper  $\sigma$  for each domain based on the shadow models.

## 5.2 Evaluation of CBD Detection

Here, we show the detection performance of CBD against backdoor attacks with various trigger types, including the BadNet square [18], the "chessboard" (CB) pattern [75], and the blended pattern [8]. For each of GTSRB, SVHN, and CIFAR-10, we train 20 models (using the full training set) for each trigger type following the same training configurations described in Sec. 5.1.1. TinyImageNet is not considered here due to the high training cost. Details for each trigger type and attack settings are shown in App. C.4. We also compare CBD with three state-of-the-art backdoor detectors without certification, which are Neural Cleanse (NC) [67], K-Arm [56], and MNTD [82]. In particular, K-Arm and MNTD require manual selection of the detection threshold. For both of them, we choose the threshold that maximizes the TPR while keeping a 5% FPR for each dataset. Moreover, we devise a "supervised" version of CBD, named CBD<sub>sup</sub>, which still uses LDP as the detection statistic but without the conformal prediction. The detection threshold for CBD<sub>sup</sub> is determined in the same way as for K-Arm and MNTD, i.e. by maximizing the TPR with a controlled 5% FPR.

In practice, CBD needs to choose a moderately large  $\sigma$  for each detection task. To this end, we first initialize a small  $\sigma$  such that for each of the N shadow models, the SLPVs for the K samples used for computing the LDP all concentrate at the labeled classes. In this case, the LDPs for all the shadow models are close to  $\frac{1}{K}$ . Then, we gradually increase  $\sigma$  until  $\frac{1}{N \times K} \sum_{n=1}^{N} \sum_{k=1}^{K} p_k(x_k^{(n)} | w_n, \sigma) < \psi$  for some relatively small  $\psi$ , where  $x^{(n)}$  is the k-th sample for LDP computation for the n-th model, i.e. the SLPVs are no longer concentrated at the labeled classes. In the left of Fig. 4, we show the choice of  $\sigma$  based on the above scheme for a range of  $\psi$ , which exhibits a trend of convergence as  $\psi$  decreases. We also notice that  $\sigma$  selected for  $\psi < 0.2$  roughly matches the  $\sigma$  choices in Fig. 2 that yields relatively high CTPR and TPR, showing the effectiveness of our scheme. In our evaluation of CBD detection, we set  $\psi = 0.1$ , which yields  $\sigma = 1.15, 0.39, 1.14$  for GTSRB, SVHN, and CIFAR-10, respectively. Other choices of  $\sigma$  for  $\psi$  less than 0.2 yield similar detection performance.

As shown in Tab. 1, CBD achieves comparable or even higher TPRs than the SOTA detectors (that benefit from unrealistic supervision) for all trigger types on all datasets. CBD also provides non-trivial detection guarantees to most attack types on these datasets. The relatively low CTPRs, e.g. for BadNet on GTSRB, are due to the large perturbation magnitude of the trigger. The even better TPRs achieved by CBD<sub>sup</sub>, though with the same supervision as for the SOTA detectors, show the effectiveness of the LDP statistic in distinguishing backdoored models from benign ones. Such effectiveness is further verified by the receiver operating characteristic (ROC) curves for CBD<sub>sup</sub>. Compared with the baseline detectors, CBD<sub>sup</sub> achieves generally higher overall areas under curves (AUCs) across the three datasets.

## 5.3 Ablation Study

We show that the time efficiency and data efficiency of CBD can be improved by training fewer shadow models and using fewer samples for training the shadow models, respectively, without significant degradation in the detection or certification performance. In particular, we show in Tab. 2 that CBD with  $\beta = 0.2$  achieves similar TPRs and CTPRs for the same set of attacks in Sec. 5.2 when we reduce the number of shadow models from 100 to 50, 25, and 10, respectively. Such robustness of CBD to the calibration size further verifies the clear separation between the benign and backdoored classifiers using our proposed LDP. In Tab. 3, we show that with shadow models trained on only 100

Table 1: Certified detection of CBD for  $\beta = 0, 0.1, 0.2$  (shaded), with the empirical detection performance (measured by TPR (%)) compared with NC, K-Arm, MNTD, and CBD<sub>sup</sub> against BadNet, CB, and Blend attacks on GTSRB, SVHN, and CIFAR-10. The parentheses in each shaded cell contain the CTPR (%) associated with the TPR outside the parentheses. CBD achieves comparable or even higher empirical TPRs compared with the SOTA baselines and provides non-trivial (or even tight) certification for different attacks and datasets. FPRs (%) are reported on benign classifiers.

		GTSRB				S	VHN			Average			
	benign	BadNet	CB	Blend	benign	BadNet	CB	Blend	benign	BadNet	CB	Blend	TPR
NC	20	50	75	20	40	80	100	95	20	35	95	60	67.8
K-Arm	5	100	100	100	5	100	70	40	5	100	80	55	82.8
MNTD	5	20	0	0	5	10	10	15	5	90	100	75	35.6
<b>CBD</b> <sub>sup</sub>	5	100	95	100	5	100	100	90	5	65	100	55	89.4
$CBD_0$	0	75 (5)	95 (80)	80 (20)	0	75 (45)	100 (100)	80 (75)	0	50 (5)	100 (90)	45 (30)	77.2
$CBD_{0.1}$	0	90 (15)	95 (85)	90 (25)	0	90 (55)	100 (100)	80 (80)	20	75 (20)	100 (95)	55 (35)	86.1
CBD <sub>0.2</sub>	0	90 (15)	95 (85)	95 (35)	0	95 (65)	100 (100)	90 (80)	25	75 (25)	100 (100)	60 (40)	88.9



Figure 3: Receiver operating characteristic (ROC) curves of CBD<sub>sup</sub> aggregated over all three trigger types on GTSRB, SVNH, and CIFAR-10, respectively. CBD<sub>sup</sub> with our proposed LDP statistic achieves higher overall areas under curves (AUCs) than K-Arm and MNTD across the three datasets.

Table 2: Certified detection of CBD (with CTPR inside the parentheses and TPR outside) for  $\beta = 0.2$  using 10, 25, 50, and 100 (the default in Sec. 5.2) shadow models. Both the detection and certification performance of CBD are not significantly affected by reducing the number of shadow models.

		GT	SRB			S	VHN		CIFAR-10				
# shadow	benign	BadNet	CB	Blend	benign	BadNet	CB	Blend	benign	BadNet	CB	Blend	
10	0	95 (10)	95 (85)	95 (35)	0	75 (45)	100 (100)	90 (75)	25	85 (25)	100 (100)	55 (40)	
25	0	95 (5)	95 (85)	95 (25)	0	95 (45)	100 (100)	80 (75)	25	80 (25)	100 (100)	70 (40)	
50	0	95 (15)	95 (85)	95 (40)	0	95 (65)	100 (100)	85 (75)	25	80 (25)	100 (100)	60 (40)	
100	0	90 (15)	95 (85)	95 (35)	0	95 (65)	100 (100)	90 (80)	25	75 (25)	100 (100)	60 (40)	

Table 3: Certified detection of CBD (with CTPR inside the parentheses and TPR outside) for  $\beta = 0.2$ and  $\beta = 0.4$ , respectively, with 100 shadow models trained on fewer samples (100 per class) than the default settings in Sec. 5.2. Due to the significantly insufficient training of the shadow models, a larger  $\beta$  is needed to maintain a similar level of TPR and CTPR as in Sec. 5.2.

		GT	SRB			S	VHN		CIFAR-10			
	benign	BadNet	CB	Blend	benign	BadNet	CB	Blend	benign	BadNet	CB	Blend
CBD <sub>0.2</sub>	0	90 (5)	95 (85)	90 (25)	0	75 (45)	100 (95)	80 (75)	0	35 (0)	95 (90)	45 (40)
CBD <sub>0.4</sub>	0	95 (5)	95 (85)	95 (35)	0	95 (45)	100 (100)	85 (75)	5	60 (10)	100 (95)	55 (40)

clean samples per class, CBD requires a larger  $\beta$  to achieve similar TPRs and CTPRs. This is because more shadow models will exhibit an abnormally large LDP due to significantly insufficient training.

#### 5.4 Additional Experiments

**Empirical validation of the stochastic dominance assumption in Thm. 4.2.** In the middle of Fig. 4, we show the histograms (with the associated empirical CDF) of the LDP statistics for the shadow models and the benign models for all four datasets. The statistics for each dataset are obtained using the practically selected  $\sigma$ . The LDP for the benign models is clearly dominated by the LDP for the shadow models in the sense of first-order stochastic dominance.



Figure 4: Supportive results: (Left) Choice of  $\sigma$  for a range of  $\psi$  based on our selection scheme, which matches the  $\sigma$  choices in Fig. 2 with high CTPR and TPR. (Middle) The histograms of the LDP statistics for the shadow models and the benign models, with the associated empirical CDFs. LDP for benign models is stochastically dominated by the LDP for shadow models for all datasets. (**Right**) Vulnerability of WaNet attack on GTSRB and SVHN. Attack success rate (ASR) reduces with a negligible drop in benign accuracy (ACC) when inputs are smoothed by Gaussian noise.

Class imbalance is not the reason for a large LDP. In our experiments involving generally balanced datasets, backdoor poisoning (i.e. embedding the trigger in a large variety of samples during training) not only enhances the trigger robustness of the attack, but also introduces an imbalance in the poisoned training set. Thus, it is important to show that the large LDPs observed in our experiments are a result of the robustness of the trigger, rather than the class imbalance. Note that if class imbalance can also cause a large LDP, there will easily be false alarms for benign classifiers trained on imbalanced datasets<sup>1</sup>. Here, we train two groups of benign models on SVHN, with 20 models per group. For the first group, the models are trained on a balanced dataset with 3,000 images per class. For each model in the second group, the training set contains 4,400 additional images labeled to some randomly selected class. With the same model architecture and training configurations, the two groups have similar LDP distributions, with mean $\pm$ std being 0.445 $\pm$ 0.125 and 0.429 $\pm$ 0.119, respectively, and with a 0.698 p-value for the t-test for mean. Thus, LDP will not be affected by class imbalance in general, and our method indeed detects the backdoor attack rather than the class imbalance.

Advanced attacks. Based on the key ideas in Sec. 1, CBD requires the attack to have a large STR over the sample distribution. However, this requirement is not always satisfied, especially for some advanced attacks with subtle, sample-specific triggers, such as WaNet [51]. Although not detectable or certifiable by our CBD, these attacks can hardly survive noises either from the environment or simple prepossessing-based defenses in practice. To see this, for each of GTSRB and SVHN, we train 20 models with successful WaNet attacks. We consider a simple test-time defense by applying 1024 randomly sampled Gaussian noises from distribution  $\mathcal{N}(0, \sigma^2 I)$  to each input and then performing a majority vote. As shown in the right of Fig. 4, for both datasets and for small  $\sigma$ , the average attack success rate (ASR) quickly drops without clear scarifies in the benign accuracy (ACC).

## 6 Conclusion

In this paper, we proposed CBD, the first certified backdoor detector, which is based on an adjustable conformal prediction using a novel LDP statistic. CBD not only performs detection inference but also provides a condition for attacks that are guaranteed to be detectable. Our theoretical results show that backdoor attacks with a trigger more resilient to noises and with a smaller perturbation magnitude are more likely to be detected with a guarantee. Our empirical results show the strong certification and detection performance of CBD on four benchmark datasets. In future research, we aim to enhance the certification bound to encompass backdoor attacks with larger trigger perturbation norms, such as rotational triggers and subject-based triggers.

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<sup>&</sup>lt;sup>1</sup>This is the case for the backdoor detector in [68] which leverages the overfitting to the backdoor trigger during training – benign classifiers trained on imbalanced datasets will also easily trigger a (false) detection.

## References

- [1] Model Zoo. https://modelzoo.co/.
- [2] Anastasios N. Angelopoulos and Stephen Bates. A gentle introduction to conformal prediction and distribution-free uncertainty quantification. 2021.
- [3] Hamed Pirsiavash Aniruddha Saha, Akshayvarun Subramanya. Hidden trigger backdoor attacks. In AAAI Conference on Artificial Intelligence (AAAI), 2020.
- [4] Eitan Borgnia, Jonas Geiping, Valeriia Cherepanova, Liam Fowl, Arjun Gupta, Amin Ghiasi, Furong Huang, Micah Goldblum, and Tom Goldstein. DP-InstaHide: Provably Defusing Poisoning and Backdoor Attacks with Differentially Private Data Augmentations. In ICLR Workshop on Security and Safety in Machine Learning Systems, March 2021.
- [5] Bryant Chen, Wilka Carvalho, Nathalie Baracaldo, Heiko Ludwig, Benjamin Edwards, Taesung Lee, Ian Molloy, and Biplav Srivastava. Detecting backdoor attacks on deep neural networks by activation clustering. http://arxiv.org/abs/1811.03728, Nov 2018.
- [6] Huili Chen, Cheng Fu, Jishen Zhao, and Farinaz Koushanfar. DeepInspect: A black-box trojan detection and mitigation framework for deep neural networks. In *International Joint Conference* on Artificial Intelligence (IJCAI), pages 4658–4664, 7 2019.
- [7] Pin-Yu Chen, Huan Zhang, Yash Sharma, Jinfeng Yi, and Cho-Jui Hsieh. Zoo: Zeroth order optimization based black-box attacks to deep neural networks without training substitute models. In ACM Workshop on Artificial Intelligence and Security (AISec), page 15–26, 2017.
- [8] Xinyun Chen, Chang Liu, Bo Li, Kimberly Lu, and Dawn Song. Targeted backdoor attacks on deep learning systems using data poisoning. https://arxiv.org/abs/1712.05526v1, 2017.
- [9] Edward Chou, Florian Tramèr, and Giancarlo Pellegrino. Sentinet: Detecting localized universal attacks against deep learning systems. In 2020 IEEE Security and Privacy Workshops (SPW), pages 48–54. IEEE, 2020.
- [10] Jeremy Cohen, Elan Rosenfeld, and Zico Kolter. Certified adversarial robustness via randomized smoothing. In *Proceedings of the 36th International Conference on Machine Learning*, pages 1310–1320, 2019.
- [11] Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *IEEE Conference on Computer Vision and Pattern Recognition* (CVPR), pages 248–255, 2009.
- [12] Bao Gia Doan, Ehsan Abbasnejad, and Damith C. Ranasinghe. Februus: Input purification defense against trojan attacks on deep neural network systems. In *Annual Computer Security Applications Conference (ACSAC)*, page 897–912, 2020.
- [13] Yinpeng Dong, Xiao Yang, Zhijie Deng, Tianyu Pang, Zihao Xiao, Hang Su, and Jun Zhu. Black-box detection of backdoor attacks with limited information and data. In *Proceedings of the IEEE/CVF International Conference on Computer Vision (ICCV)*, 2021.
- [14] Min Du, Ruoxi Jia, and Dawn Song. Robust anomaly detection and backdoor attack detection via differential privacy. In *International Conference on Learning Representations (ICLR)*, 2020.
- [15] Yansong Gao, Change Xu, Derui Wang, Shiping Chen, Damith C. Ranasinghe, and Surya Nepal. STRIP: A defence against trojan attacks on deep neural networks. In *Annual Computer Security Applications Conference (ACSAC)*, 2019.
- [16] Jonas Geiping, Liam Fowl, Gowthami Somepalli, Micah Goldblum, Michael Moeller, and Tom Goldstein. What doesn't kill you makes you robust(er): Adversarial training against poisons and backdoors. In ICLR 2021 Workshop on Security and Safety in Machine Learning Systems, 2021.
- [17] Ian J. Goodfellow, Jonathon Shlens, and Christian Szegedy. Explaining and harnessing adversarial examples. In *International Conference on Learning Representations (ICLR)*, 2015.

- [18] Tianyu Gu, Kang Liu, Brendan Dolan-Gavitt, and Siddharth Garg. Badnets: Evaluating backdooring attacks on deep neural networks. *IEEE Access*, 7:47230–47244, 2019.
- [19] Jiyang Guan, Zhuozhuo Tu, Ran He, and Dacheng Tao. Few-shot backdoor defense using shapley estimation. In CVPR, 2022.
- [20] Wenbo Guo, Lun Wang, Xinyu Xing, Min Du, and Dawn Song. TABOR: A highly accurate approach to inspecting and restoring Trojan backdoors in AI systems. https://arxiv.org/abs/1908.01763, 2019.
- [21] Frank R. Hampel. The influence curve and its role in robust estimation. *Journal of the American Statistical Association*, 69, 1974.
- [22] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2016.
- [23] Sanghyun Hong, Varun Chandrasekaran, Yiğitcan Kaya, Tudor Dumitraş, and Nicolas Papernot. On the effectiveness of mitigating data poisoning attacks with gradient shaping. https://arxiv.org/abs/2002.11497, 2020.
- [24] Xiaoling Hu, Xiao Lin, Michael Cogswell, Yi Yao, Susmit Jha, and Chao Chen. Trigger hunting with a topological prior for trojan detection. In *International Conference on Learning Representations*, 2022.
- [25] Kunzhe Huang, Yiming Li, Baoyuan Wu, Zhan Qin, and Kui Ren. Backdoor defense via decoupling the training process. In *International Conference on Learning Representations* (*ICLR*), 2022.
- [26] Andrew Ilyas, Sung Min Park, Logan Engstrom, Guillaume Leclerc, and Aleksander Madry. Datamodels: Predicting predictions from training data, 2022.
- [27] Jinyuan Jia, Yupei Liu, Xiaoyu Cao, and Neil Zhenqiang Gong. Certified robustness of nearest neighbors against data poisoning and backdoor attacks. In AAAI Conference on Artificial Intelligence, 2020.
- [28] Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization. In International Conference on Learning Representations (ICLR), 2015.
- [29] Soheil Kolouri, Aniruddha Saha, Hamed Pirsiavash, and Heiko Hoffmann. Universal litmus patterns: Revealing backdoor attacks in cnns. In *IEEE/CVF Conference on Computer Vision* and Pattern Recognition (CVPR), pages 298–307, 2020.
- [30] Alex Krizhevsky. Learning multiple layers of features from tiny images. *University of Toronto*, 05 2012.
- [31] Leaderboard. GTSRB Leaderboard. https://www.kaggle.com/c/nyu-cv-fall-2018/ leaderboard, 2018.
- [32] Mathias Lecuyer, Vaggelis Atlidakis, Roxana Geambasu, Daniel Hsu, and Suman Jana. Certified robustness to adversarial examples with differential privacy. In 2019 IEEE Symposium on Security and Privacy (SP), 2019.
- [33] Linyi Li, Tao Xie, and Bo Li. SoK: Certified Robustness for Deep Neural Networks. In 44th IEEE Symposium on Security and Privacy, San Francisco, CA, 2023.
- [34] Xi Li, Zhen Xiang, David J. Miller, and George Kesidis. Test-time detection of backdoor triggers for poisoned deep neural networks. In ICASSP 2022 - 2022 IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP), 2022.
- [35] Yige Li, Xixiang Lyu, Nodens Koren, Lingjuan Lyu, Bo Li, and Xingjun Ma. Neural Attention Distillation: Erasing Backdoor Triggers from Deep Neural Networks. In *International Conference on Learning Representations (ICLR)*, 2021.
- [36] Yiming Li, Yong Jiang, Zhifeng Li, and Shu-Tao Xia. Backdoor learning: A survey. *IEEE Transactions on Neural Networks and Learning Systems*, pages 1–18, 2022.

- [37] Yuezun Li, Yiming Li, Baoyuan Wu, Longkang Li, Ran He, and Siwei Lyu. Invisible backdoor attack with sample-specific triggers. In *IEEE International Conference on Computer Vision* (*ICCV*), 2021.
- [38] Cong Liao, Haoti Zhong, Anna Squicciarini, Sencun Zhu, and David Miller. Backdoor embedding in convolutional neural network models via invisible perturbation. In CODASPY, 2020.
- [39] Ji Lin, Chuang Gan, and Song Han. Defensive quantization: When efficiency meets robustness. In *International Conference on Learning Representations (ICLR)*, 2019.
- [40] Kang Liu, Brendan Dolan-Gavitt, and Siddharth Garg. Fine-pruning: Defending against backdoor attacks on deep neural networks. In *International Symposium on Research in Attacks, Intrusions, and Defenses (RAID)*, 2018.
- [41] Yingqi Liu, Wen-Chuan Lee, Guanhong Tao, Shiqing Ma, Yousra Aafer, and Xiangyu Zhang. ABS: Scanning neural networks for back-doors by artificial brain stimulation. In ACM SIGSAC Conference on Computer and Communications Security (CCS), page 1265–1282, 2019.
- [42] Yingqi Liu, Shiqing Ma, Yousra Aafer, Wen-Chuan Lee, Juan Zhai, Weihang Wang, and Xiangyu Zhang. Trojaning attack on neural networks. In *Network and Distributed System Security (NDSS) Symposium*, San Diego, CA, 2018.
- [43] Yunfei Liu, Xingjun Ma, James Bailey, and Feng Lu. Reflection Backdoor: A Natural Backdoor Attack on Deep Neural Networks. In European Conference on Computer Vision (ECCV), 2020.
- [44] Wanlun Ma, Derui Wang, Ruoxi Sun, Minhui Xue, Sheng Wen, and Yang Xiang. The "beatrix" resurrections: Robust backdoor detection via gram matrices. arXiv preprint arXiv:2209.11715, 2022.
- [45] Aleksander Madry, Aleksandar Makelov, Ludwig Schmidt, Dimitris Tsipras, and Adrian Vladu. Towards deep learning models resistant to adversarial attacks. In *International Conference on Learning Representations (ICLR)*, 2018.
- [46] David J. Miller, Zhen Xiang, and George Kesidis. Adversarial learning in statistical classification: A comprehensive review of defenses against attacks. *Proceedings of the IEEE*, 108:402–433, 2020.
- [47] Yuval Netzer, Tao Wang, Adam Coates, Alessandro Bissacco, Bo Wu, and Andrew Y. Ng. Reading digits in natural images with unsupervised feature learning. In NIPS Workshop on Deep Learning and Unsupervised Feature Learning 2011, 2011.
- [48] NeurIPS. Trojan Detection Challenge NeurIPS 2022. https://trojandetection.ai/, 2022.
- [49] Jerzy Neyman and Egon S. Pearson. On the problem of the most efficient tests of statistical hypotheses. *Philosophical Transactions of the Royal Society of London. Series A, Containing Papers of a Mathematical or Physical Character*, 231:289–337, 1933.
- [50] Anh Nguyen and Anh Tran. Input-aware dynamic backdoor attack. In *Proceedings of Advances* in Neural Information Processing Systems (NeurIPS), 2020.
- [51] Anh Nguyen and Anh Tran. Wanet imperceptible warping-based backdoor attack. In *International Conference on Learning Representations (ICLR)*, 2021.
- [52] David Wagner Nicholas Carlini. Towards evaluating the robustness of neural networks. In *IEEE Symposium on Security and Privacy (SP)*, pages 39–57, May 2017.
- [53] Elan Rosenfeld, Ezra Winston, Pradeep Ravikumar, and J. Zico Kolter. Certified robustness to label-flipping attacks via randomized smoothing. In *Proceedings of the 37th International Conference on Machine Learning*, 2020.
- [54] Mark Sandler, Andrew Howard, Menglong Zhu, Andrey Zhmoginov, and Liang-Chieh Chen. Inverted residuals and linear bottlenecks: Mobile networks for classification, detection and segmentation. In *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2018.

- [55] Esha Sarkar, Yousif Alkindi, and Michail Maniatakos. Backdoor suppression in neural networks using input fuzzing and majority voting. *IEEE Design & Test*, 37(2):103–110, 2020.
- [56] Guangyu Shen, Yingqi Liu, Guanhong Tao, Shengwei An, Qiuling Xu, Siyuan Cheng, Shiqing Ma, and Xiangyu Zhang. Backdoor Scanning for Deep Neural Networks through K-Arm Optimization. In *International Conference on Machine Learning (ICML)*, 2021.
- [57] Yanyao Shen and Sujay Sanghavi. Learning with bad training data via iterative trimmed loss minimization. In *International Conference on Machine Learning (ICML)*, pages 5739–5748, 2019.
- [58] Gagandeep Singh, Timon Gehr, Matthew Mirman, Markus Püschel, and Martin Vechev. Fast and effective robustness certification. In *Advances in Neural Information Processing Systems*, 2018.
- [59] Gagandeep Singh, Timon Gehr, Markus Püschel, and Martin Vechev. Robustness certification with refinement. In *International Conference on Learning Representations*, 2019.
- [60] Johannes Stallkamp, Marc Schlipsing, Jan Salmen, and Christian Igel. Man vs. computer: Benchmarking machine learning algorithms for traffic sign recognition. *Neural Networks*, 32:323–332, 2012.
- [61] Christian Szegedy, Wojciech Zaremba, Ilya Sutskever, Joan Bruna, Dumitru Erhan, Ian Goodfellow, and Rob Fergus. Intriguing properties of neural networks. In *International Conference* on Learning Representations (International Conference on Learning Representations (ICLR)), 2014.
- [62] Guanhong Tao, Guangyu Shen, Yingqi Liu, Shengwei An, Qiuling Xu, Shiqing Ma, Pan Li, and Xiangyu Zhang. Better trigger inversion optimization in backdoor scanning. In 2022 Conference on Computer Vision and Pattern Recognition (CVPR 2022), 2022.
- [63] Brandon Tran, Jerry Li, and Aleksander Madry. Spectral signatures in backdoor attacks. In *Advances in Neural Information Processing Systems (NIPS)*, 2018.
- [64] IARPA TrojAI: Trojans in artificial intelligence. https://www.iarpa.gov/index.php/researchprograms/trojai/trojai-baa, 2019.
- [65] Alexander Turner, Dimitris Tsipras, and Aleksander Madry. Clean-label backdoor attacks. https://people.csail.mit.edu/madry/lab/cleanlabel.pdf, 2019.
- [66] Vladimir Vovk. Conditional validity of inductive conformal predictors. In *Proceedings of the Asian Conference on Machine Learning*, pages 475–490, 04–06 Nov 2012.
- [67] Bolun Wang, Yuanshun Yao, Shawn Shan, Huiying Li, Bimal Viswanath, Haitao Zheng, and Ben Y. Zhao. Neural cleanse: Identifying and mitigating backdoor attacks in neural networks. In *IEEE Symposium on Security and Privacy (SP)*, 2019.
- [68] Hang Wang, Zhen Xiang, David J Miller, and George Kesidis. Mm-bd: Post-training detection of backdoor attacks with arbitrary backdoor pattern types using a maximum margin statistic. In 2024 IEEE Symposium on Security and Privacy (SP), 2024.
- [69] Ren Wang, Gaoyuan Zhang, Sijia Liu, Pin-Yu Chen, Jinjun Xiong, and Meng Wang. Practical detection of trojan neural networks: Data-limited and data-free cases. In *European Conference* on Computer Vision (ECCV), 2020.
- [70] Zhenting Wang, Juan Zhai, and Shiqing Ma. Bppattack: Stealthy and efficient trojan attacks against deep neural networks via image quantization and contrastive adversarial learning. In IEEE Conference on Computer Vision and Pattern Recognition (CVPR), 2022.
- [71] Maurice Weber, Xiaojun Xu, Bojan Karlaš, Ce Zhang, and Bo Li. Rab: Provable robustness against backdoor attacks. In 2023 2023 IEEE Symposium on Security and Privacy (SP) (SP), pages 640–657, 2023.
- [72] Dongxian Wu and Yisen Wang. Adversarial neuron pruning purifies backdoored deep models. In *NeurIPS*, 2021.

- [73] Zhen Xiang, David J. Miller, Siheng Chen, Xi Li, and George Kesidis. Detecting backdoor attacks against point cloud classifiers. In *IEEE International Conference on Acoustics, Speech* and Signal Processing (ICASSP), 2022.
- [74] Zhen Xiang, David J. Miller, and George Kesidis. A benchmark study of backdoor data poisoning defenses for deep neural network classifiers and a novel defense. In *IEEE MLSP*, Pittsburgh, 2019.
- [75] Zhen Xiang, David J. Miller, and George Kesidis. Detection of backdoors in trained classifiers without access to the training set. *IEEE Transactions on Neural Networks and Learning Systems*, pages 1–15, 2020.
- [76] Zhen Xiang, David J. Miller, and George Kesidis. L-RED: Efficient post-training detection of imperceptible backdoor attacks without access to the training set. In *IEEE International Conference on Acoustics, Speech and Signal Processing (ICASSP)*, pages 3745–3749, 2021.
- [77] Zhen Xiang, David J. Miller, and George Kesidis. Reverse engineering imperceptible backdoor attacks on deep neural networks for detection and training set cleansing. *Computers and Security*, 106, 2021.
- [78] Zhen Xiang, David J. Miller, and George Kesidis. Post-training detection of backdoor attacks for two-class and multi-attack scenarios. In *International Conference on Learning Representations* (*ICLR*), 2022.
- [79] Zhen Xiang, David J. Miller, Hang Wang, and George Kesidis. Detecting scene-plausible perceptible backdoors in trained DNNs without access to the training set. *Neural Computation*, 33(5):1329–1371, 2021.
- [80] Zhen Xiang, Zidi Xiong, and Bo Li. Umd: Unsupervised model detection for x2x backdoor attacks. In *Proceedings of the 40th International Conference on Machine Learning*, 2023.
- [81] Weilin Xu, David Evans, and Yanjun Qi. Feature squeezing: Detecting adversarial examples in deep neural networks. In *Network and Distributed System Security (NDSS) Symposium*, 2018.
- [82] Xiaojun Xu, Qi Wang, Huichen Li, Nikita Borisov, Carl A. Gunter, and Bo Li. Detecting AI Trojans using meta neural analysis. In *IEEE Symposium on Security and Privacy (SP)*, 2021.
- [83] Mingfu Xue, Can He, Jian Wang, and Weiqiang Liu. One-to-n & n-to-one: Two advanced backdoor attacks against deep learning models. *IEEE Transactions on Dependable and Secure Computing*, 19(3):1562–1578, 2022.
- [84] Mingfu Xue, Shifeng Ni, Yinghao Wu, Yushu Zhang, Jian Wang, and Weiqiang Liu. Imperceptible and multi-channel backdoor attack against deep neural networks, 2022.
- [85] Yi Zeng, Si Chen, Won Park, Z. Morley Mao, Ming Jin, and Ruoxi Jia. Adversarial unlearning of backdoors via implicit hypergradient. In *International Conference on Learning Representations* (ICLR), 2022.
- [86] Yuhao Zhang, Aws Albarghouthi, and Loris D'Antoni. Bagflip: A certified defense against data poisoning. In Alice H. Oh, Alekh Agarwal, Danielle Belgrave, and Kyunghyun Cho, editors, *Advances in Neural Information Processing Systems*, 2022.
- [87] Zhendong Zhao, Xiaojun Chen, Yuexin Xuan, Ye Dong, Dakui Wang, and Kaitai Liang. Defeat: Deep hidden feature backdoor attacks by imperceptible perturbation and latent representation constraints. In *IEEE Conference on Computer Vision and Pattern Recognition (CVPR)*, 2022.
- [88] Runkai Zheng, Rongjun Tang, Jianze Li, and Li Liu. Data-free backdoor removal based on channel lipschitzness. In *ECCV*, 2022.